

# Cosmology with the Sunyaev-Zel'dovich Effect

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# Outline

- (1) Some background: the CMB, inverse Compton scattering, galaxy clusters
- (2) The Sunyaev-Zel'dovich Effect
- (3) Cosmological probes
- (4) Upcoming SZ observational campaigns
- (5) Simulations of the SZE

# Outline

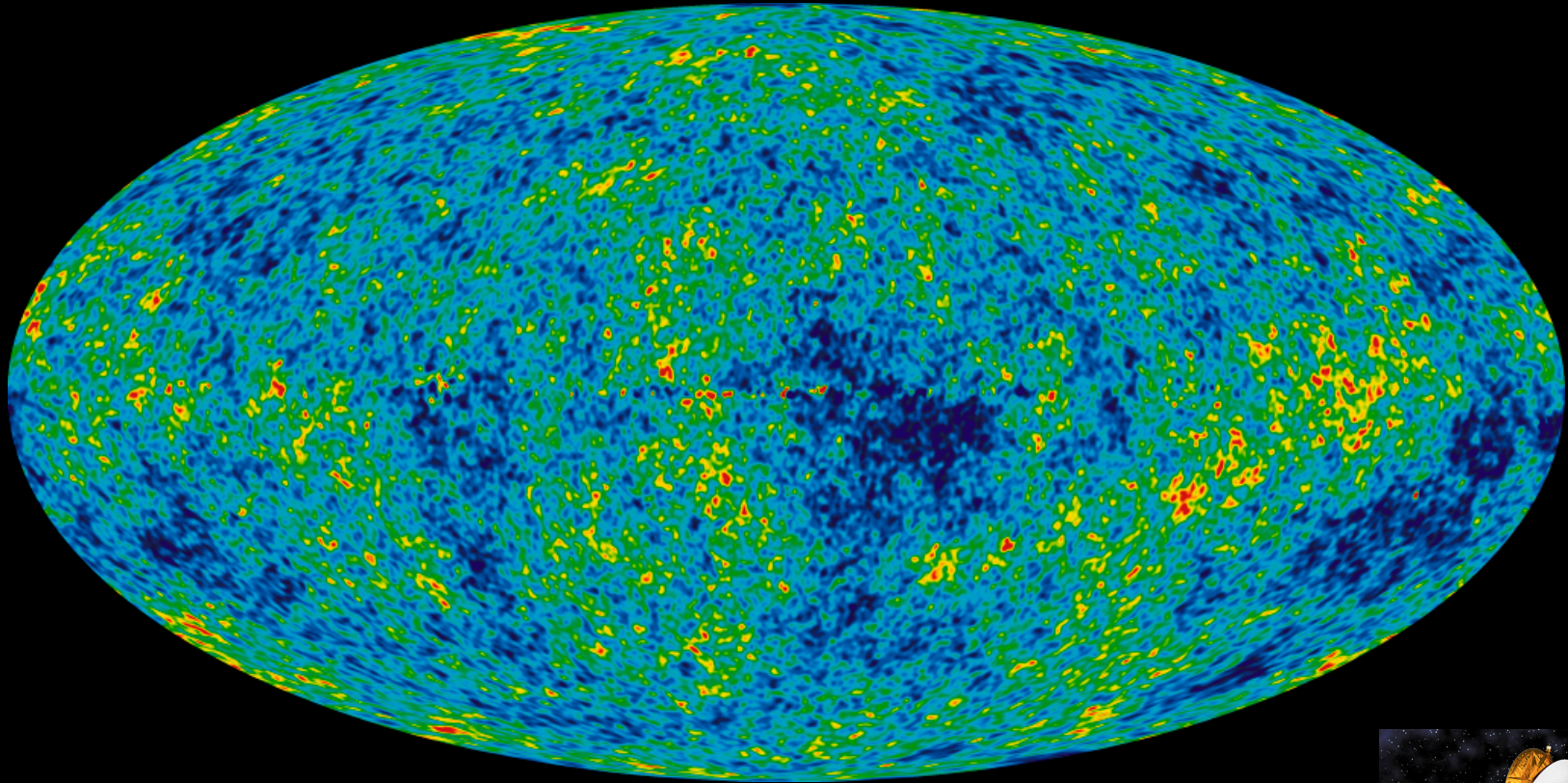
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# The cosmic microwave background

- high- $z$  ( $z \gtrsim 10^3$ ) universe was ionized, opaque due to Thompson/Coulomb scattering
- as  $T$  dropped below  $\approx 3,000$  K, hydrogen recombined and became mostly neutral
- photon mean free path went up significantly
  - universe became effectively transparent!

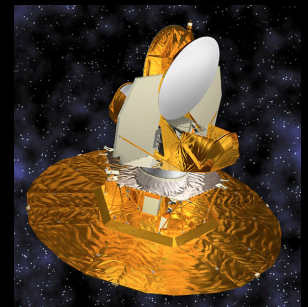


# The cosmic microwave background



WMAP Year 3 data release

image c/o NASA/WMAP science team



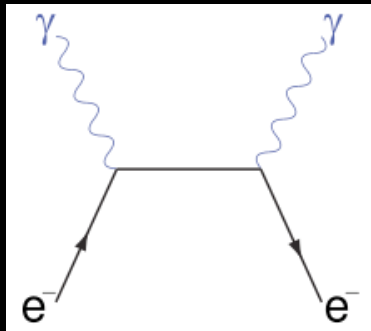
# The cosmic microwave background

- The CMB is nearly a perfect blackbody
- Acoustic peaks in CMB cause tiny fluctuations in temperature, but are still blackbody in spectrum
- There are many sources of secondary anisotropies which cause deviations from blackbody
- The CMB provides a **background light source** for these!
- These secondary anisotropies can be used to tell us many useful things about the universe!

(Example: the Sunyaev-Zel'dovich effect!)

# Inverse Compton scattering

- Nearly elastic photon-baryon scattering (photon-electron in the case we care about)
- Causes an increase of energy of a photon when it interacts with matter
- interaction in the limit of  $k_b T_e \gg h\nu$
- Very important process in many aspects of astrophysics



Single photon:

$$\varepsilon' = \frac{\varepsilon}{1 + (\varepsilon/m_e c^2)(1 - \cos \phi_{12})}$$

# Inv. Compton scattering: population of photons

Incident spectrum

$$I_0(\nu) = \frac{2h\nu^3}{c^2} (e^{h\nu/k_B T_{\text{rad}}} - 1)^{-1}$$

Output spectrum if all  
photons scattered once

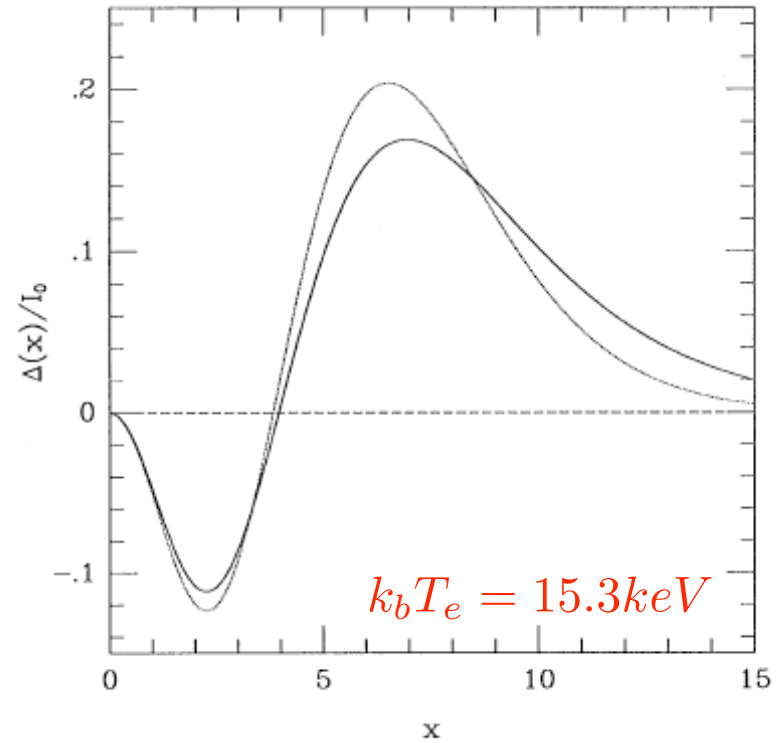
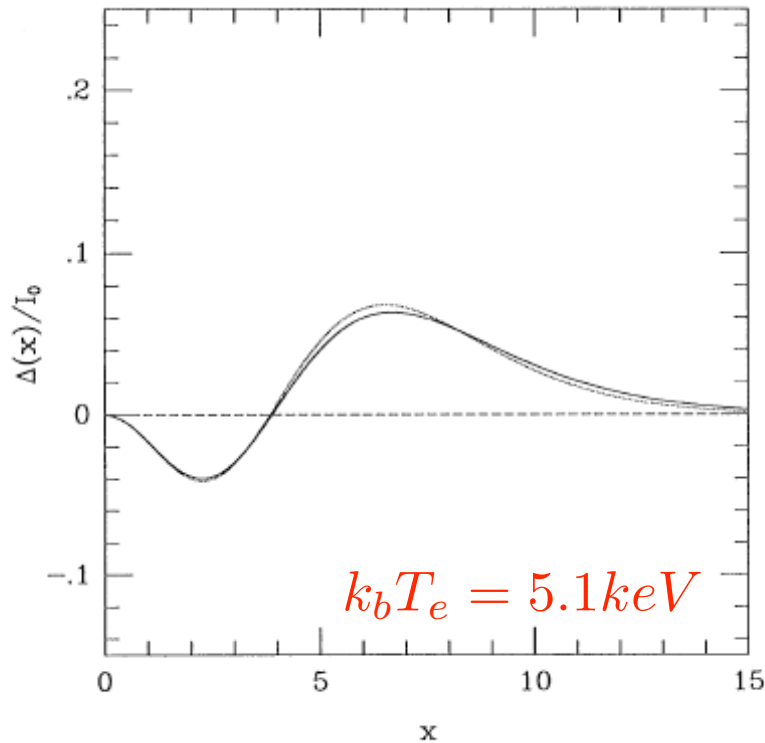
$$\frac{I(\nu)}{\nu} = \int_0^\infty d\nu_0 P_1(\nu, \nu_0) \frac{I_0(\nu_0)}{\nu_0}$$

$$\Delta I(\nu) \equiv I(\nu) - I_0(\nu) = \frac{2h}{c^2} \int_{-\infty}^\infty P_1(s) ds \left( \frac{\nu_0^3}{e^{h\nu_0/k_B T_{\text{rad}}} - 1} - \frac{\nu^3}{e^{h\nu/k_B T_{\text{rad}}} - 1} \right)$$

$P_1(s)$  = frequency shift function



## Planck spectrum scattered by thermal dist'n of electrons



$$x = \frac{h\nu}{k_b T_{rad}} = 0.0176 \frac{\nu}{\text{GHz}}$$

Note: assumes all photons scattered once!

# Galaxy clusters

- Discussed in great detail by Christoph on Tuesday (3 July)
- Largest gravitationally-bound objects in the universe
- Primarily composed of dark matter + hot ( $10^7$ - $10^8$  K) intracluster gas (also some galaxies)
- $M_{\text{char}} \sim 10^{14}$ - $10^{15} M_{\odot}$ ,  $R_{\text{char}} \sim 1$ -few Mpc,  $\langle n_b \rangle \sim 10^{-4}$

# Galaxy clusters

- Lots of interesting astrophysics going on inside galaxy clusters (c.f. Pfrommer talk)
- HOWEVER, to first order we're interested in galaxy clusters as a “big bag of gas”
- For most of talk, assume gas is approximately in hydrostatic equilibrium (not a great assumption)
- Will discuss how variations from HSE affect results later

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# The Sunyaev-Zel'dovich Effect

- Spectral distortion of the CMB caused by the scattering of CMB photons off of high-energy electrons
- Two components of SZ: thermal and kinetic
- SZE can also be polarized (though contribution is small)
- Original papers: Sunyaev & Zel'dovich  
1970 (Comm.Astrophys. Space Phys. 2:66-74),  
1972 (Comm.Astrophys. Space Phys. 4:173-78)

# Thermal SZE

- Inverse Compton scattering of CMB by thermal electron population in ICM

- Optical depth of a cluster is:

$$\tau_e \simeq n_e \sigma_T L \sim 10^{-4} - 10^{-3}$$

- only tiny fraction of CMB photons scatter - small fractional distortion of CMB!

# The thermal SZE

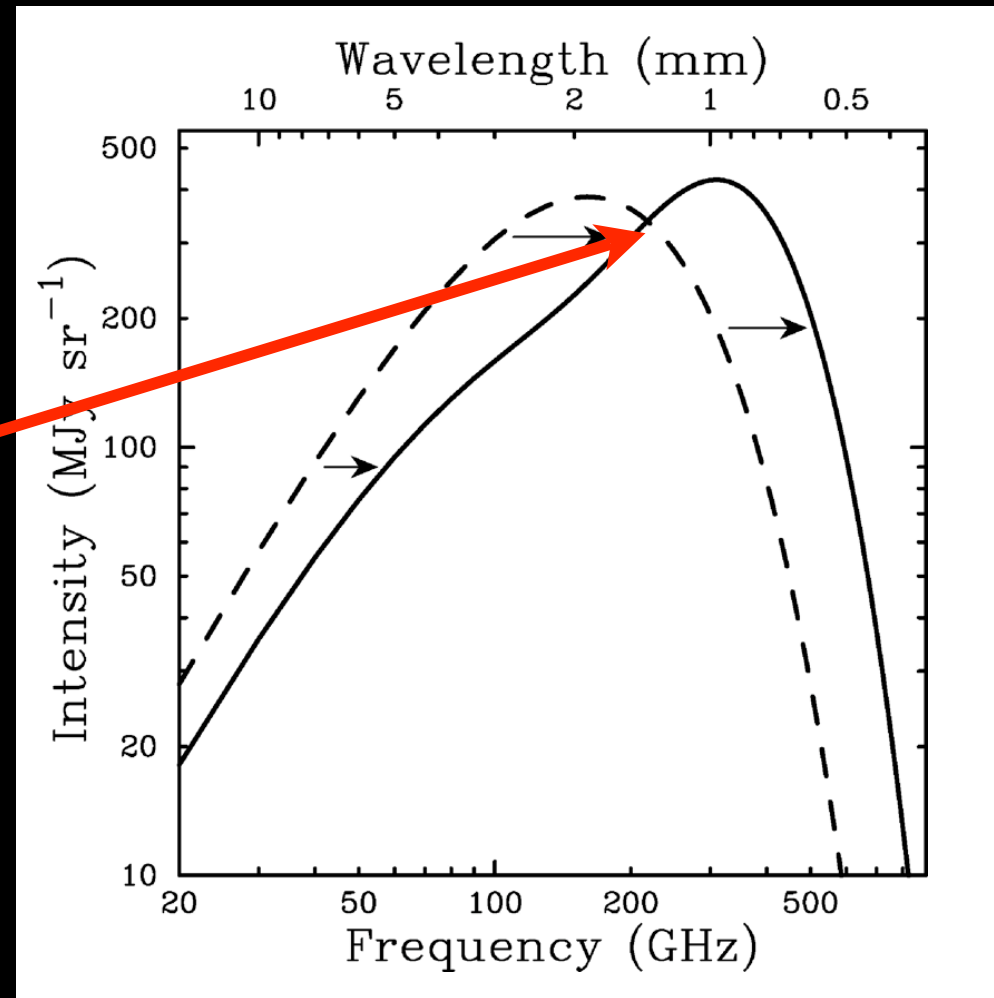
$$x \equiv \frac{h\nu}{k_B T_{CMB}}$$

$$\frac{\Delta T_{SZE}}{T_{CMB}} = f(x) \quad y = f(x) \int n_e \frac{k_B T_e}{m_e c^2} \sigma_T d\ell$$

$$f(x) = \left( x \frac{e^x + 1}{e^x - 1} - 4 \right) (1 + \delta_{SZE}(x, T_e)),$$

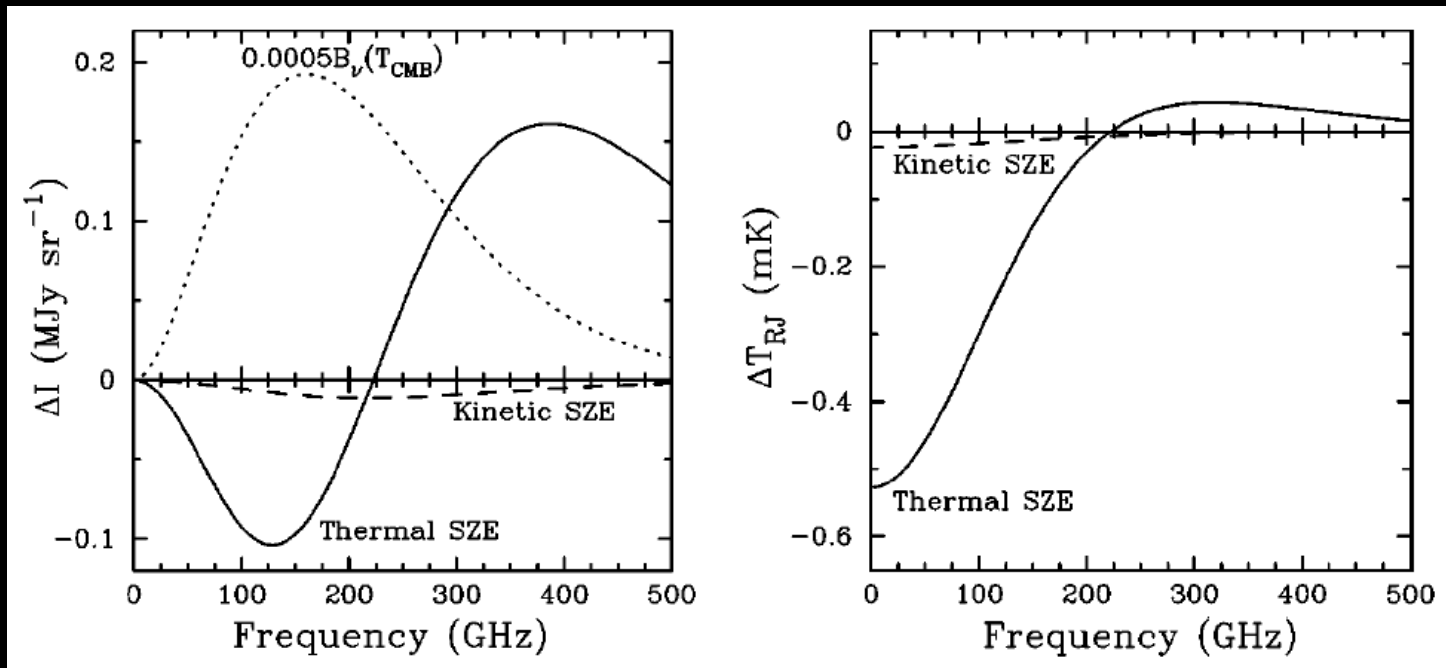
# Thermal SZE: spectral distortion

zero point ~ 218 GHz





# Thermal SZE spectral distortion



Change in CMB intensity

Change in RJ brightness  
temperature

# The integrated SZE signal

- Very important for finding clusters with an SZE survey
- Integrating over solid angle of cluster gives temperature-weighted measure of cluster electron content (and thus total thermal energy of cluster)

$$d\Omega = dA / D_A^2$$

$$\int \Delta T_{SZE} d\Omega \propto \frac{N_e \langle T_e \rangle}{D_A^2} \propto \frac{M \langle T_e \rangle}{D_A^2}$$

# Useful features of thermal SZE

- small spectral distortion of CMB which is proportional to cluster pressure along LOS
- redshift-independent
- unique spectral signature (easy to extract from back/foregrounds)
- integrated SZE flux prop. to temperature-weighted mass of cluster (mass threshold *nearly* independent of redshift)

# Kinetic SZE

- a.k.a. “Ostriker-Vishniac Effect” (O&V 1986, ApJ, 306, L51)
- If cluster is moving w.r.t. CMB rest frame, there is an additional spectral distortion due to Doppler effect of cluster bulk velocity on CMB
- LOS component of  $v_{\text{pec}}$  causes apparent change in CMB temperature!
- Kinetic SZE is still blackbody spectrum (in the nonrelativistic limit), but slightly different temperature
- This effect is rather tiny compared to thermal SZE

$$\frac{\Delta T_{\text{SZE}}}{T_{\text{CMB}}} = -\tau_e \left( \frac{v_{\text{pec}}}{c} \right)$$



# SZE polarization

- Scattering of CMB photons by ICM can result in linear polarization
- This is due to anisotropic optical depth to a given location in the cluster
- more specifically, this is due to the quadrupole component of the local radiation field (motion of cluster transverse to LOS, electron optical depth, scattering off thermal photons)

# SZE polarization

- Sunyaev & Zel'Dovich (1980, MNRAS 190: 413-420), Sazonov & Sunyaev (1999, MNRAS, 310, 765-72) - analytic spherical dist'n of clusters
  - largest terms go as  $\sim T_e(v_{\text{pec},\perp}/c)^2$  and  $\sim T_e^2(v_{\text{pec},\perp}/c)$  in CMB intensity.
  - Optimistically, polarization levels of  $\sim 10$  nK can be reached (too small!)
- Shimon et al. 2006, MNRAS 368, 511-517
  - when hydro + dm cosmological simulations are analyzed (non-symmetric, non-ideal clusters) one finds that scattering due to thermal electrons is more important than other terms
  - polarization levels of  $\sim 1$   $\mu$ K may be seen! (possibly observable)

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- (3) **Cosmological probes**
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# The SZE as a cosmological probe

- SZE is redshift-independent find clusters at wide range of  $z$  w/different selection function from other observational techniques
- Measures LOS pressure ( $n_e T_e$ ) instead of more complicated function of  $n_e, T_e$ : insensitive to cluster physics, so robust mass estimator (?)
- Can be combined with other obs. techniques to trace structure formation at the high-mass halo end from  $z \sim 2-3$  to present day!

$$\frac{\Delta T_{SZE}}{T_{CMB}} = f(x) \quad y = f(x) \int n_e \frac{k_B T_e}{m_e c^2} \sigma_T d\ell$$

# Possible cosmological probes

1. Galaxy cluster mass function/abundance evolution
2. Hubble constant and cosmological distance determination
3. Cluster gas mass fraction
4. Cluster peculiar velocities

# Galaxy cluster mass function/ abundance evolution

Press-Schechter mass function:

$$\frac{dn(M, z)}{dM} = -\sqrt{\frac{2}{\pi}} \frac{\bar{\rho}}{M^2} \frac{d \ln \sigma(M, z)}{d \ln M} \frac{\delta_c}{\sigma(M, z)} \exp \left[ \frac{-\delta_c^2}{2\sigma^2(M, z)} \right]$$

$\bar{\rho}$  = mean density of universe at present day

M = mass of halo

n = comoving number density

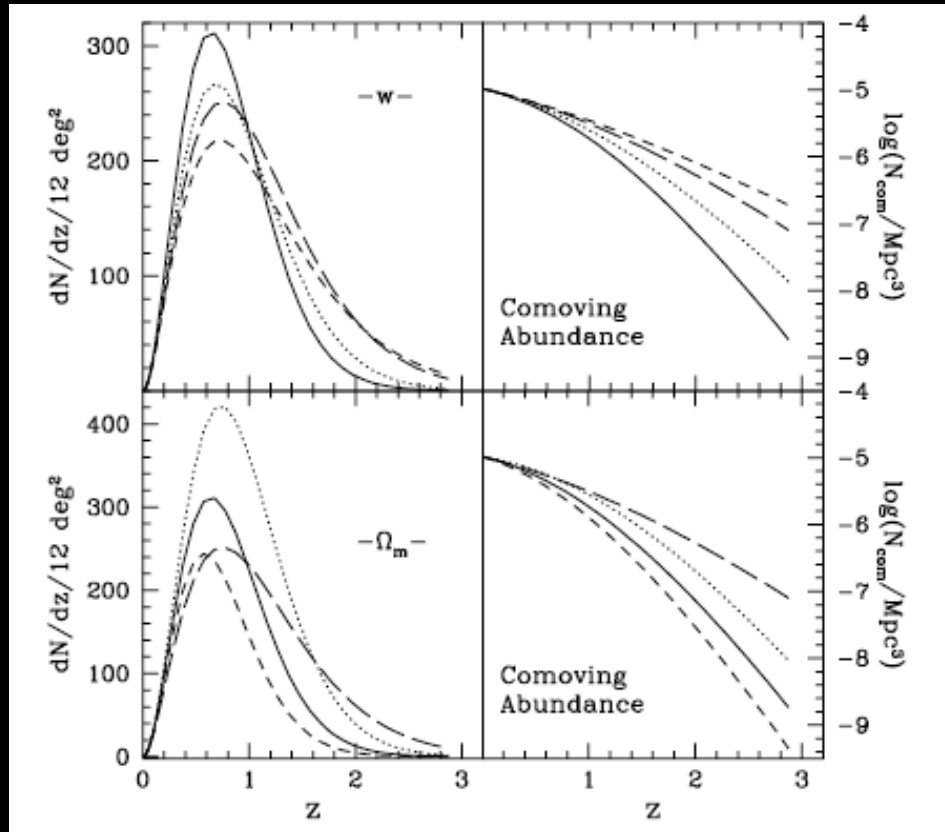
$\sigma(M, z) = \sigma(M)D(z)$  = (variance of density field)  
× (linear growth function)

$\delta_c \simeq 1.69$  = critical dens. for collapse in  
spherical collapse model

# Galaxy cluster mass function/ abundance evolution

- Galaxy cluster population is exponentially sensitive to cosmology
- Measuring, e.g.,  $N(>M)$  as a function of redshift is a very sensitive probe of cosmological parameters!
- Caveat 1: this requires a combination of SZE, some other measurements
- Caveat 2: also requires robust mass estimator (see later in talk)

# Example: variation in $w$ , $\Omega_m$ on results of an SZE survey



sfc density of clusters

comoving cluster  
abundance

solid:  $w=-1, \Omega_m=0.3, h=0.65$   
dotted, short-dashed:  
 $w = -0.6, -0.2$   
long-dashed:  $\Omega_m=0.3$

solid:  $w=-1, \Omega_m=0.3, h=0.65$   
dotted, short-dashed:  
 $\Omega_m = 0.27, 0.33$   
long-dashed:  $\Omega_m=0.3$

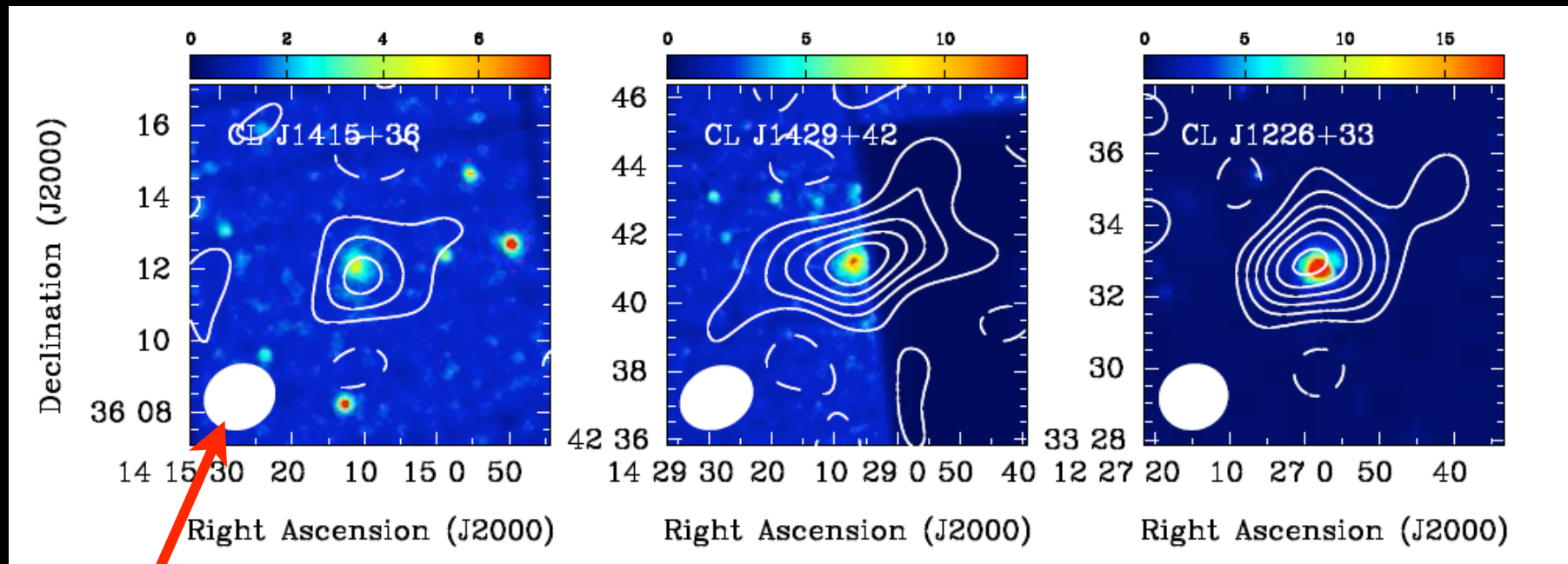
see Haiman, Mohr & Holder 2001,  
*ApJ*, 553: 545-561



# First results: The Sunyaev-Zel'dovich Array (SZA)

- Muchovej et al. 2007 (ApJ, in press; astro-ph/0610115)
- Three clusters w.  $z = 0.89-1.03$  observed at 30 GHz during commissioning period of the SZA interferometer (at BIMA site)
- Derive cluster masses assuming isothermality, hydrostatic equilibrium

# First results: The Sunyaev-Zel'dovich Array (SZA)



Beam  
FWHM

Contours: thermal SZE (SZA) @ 30 GHz  
Image: X-ray (XMM) (Maughan et al. 2006,  
MNRAS, 365, 509)

# First results: The Sunyaev-Zel'dovich Array (SZA)

Table 6. Comparison of SZ and X-ray Derived Temperature and Masses

Cluster Name	$R_{\Delta(z)}^{X-ray}$	$R$ (Mpc)	$\theta_c^b$ (")	SZ Derived Quantities			$T_e$ (keV)	X-ray Masses <sup>a</sup>	
				$T_e$ (keV)	$M_{gas}$ ( $10^{12} M_\odot$ )	$M_{total}$ ( $10^{13} M_\odot$ )		$M_{gas}$ ( $10^{12} M_\odot$ )	$M_{total}$ ( $10^{13} M_\odot$ )
Cl J1415.1+3612	$R_{2500(z)}$	0.23	11.7 [8.5, 30]	$3.7^{+0.8}_{-0.7}$	$6.2^{+1.5}_{-0.9}$	$5.6^{+1.3}_{-1.0}$	$5.7^{+1.2}_{-0.7}$	$6.7^{+1.2}_{-1.2}$	$8.8^{+3.1}_{-2.5}$
				$3.7^{+0.8}_{-0.8}$	$5.6^{+1.8}_{-0.8}$	$5.1^{+1.0}_{-1.3}$			
	$R_{200(z)}$	0.88	11.7 [8.5, 30]	$3.7^{+0.8}_{-0.7}$	$38.2^{+9.2}_{-5.5}$	$24.3^{+5.5}_{-4.3}$	$5.7^{+1.2}_{-0.7}$	$38.5^{+5.4}_{-4.3}$	$38.3^{+12.0}_{-9.4}$
Cl J1429.0+4241	$R_{2500(z)}$	0.26	12.4 [8.5, 30]	$5.5^{+0.7}_{-1.0}$	$10.8^{+1.2}_{-2.0}$	$8.9^{+1.7}_{-1.1}$	$6.2^{+1.5}_{-1.0}$	$7.3^{+1.5}_{-1.6}$	$10.5^{+4.8}_{-3.3}$
				$5.2^{+0.9}_{-0.7}$	$9.5^{+2.0}_{-1.7}$	$8.6^{+1.7}_{-1.8}$			
	$R_{200(z)}$	0.97	12.4 [8.5, 30]	$5.5^{+0.7}_{-1.0}$	$62.2^{+6.7}_{-11.2}$	$39.7^{+4.9}_{-6.7}$	$6.2^{+1.5}_{-1.0}$	$42.9^{+7.6}_{-6.0}$	$44.9^{+17.3}_{-12.9}$
Cl J1226.9+3332	$R_{2500(z)}$	0.35	14.6 [8.5, 30]	$8.9^{+1.2}_{-1.5}$	$23.7^{+3.6}_{-3.3}$	$20.9^{+2.8}_{-3.2}$	$10.6^{+1.1}_{-1.1}$	$21.5^{+1.9}_{-2.2}$	$25.0^{+4.6}_{-4.3}$
				$8.3^{+1.8}_{-0.8}$	$23.7^{+3.0}_{-4.7}$	$20.6^{+3.3}_{-3.7}$			
	$R_{200(z)}$	1.29	14.6 [8.5, 30]	$8.9^{+1.2}_{-1.5}$	$130.2^{+19.6}_{-18.3}$	$84.7^{+11.5}_{-11.5}$	$10.6^{+1.1}_{-1.1}$	$119.0^{+8.9}_{-8.2}$	$102.0^{+17.1}_{-16.8}$

<sup>a</sup>reproduced from Maughan et al. (2006)

<sup>b</sup>Prior on core radius, for SZ-derived quantities

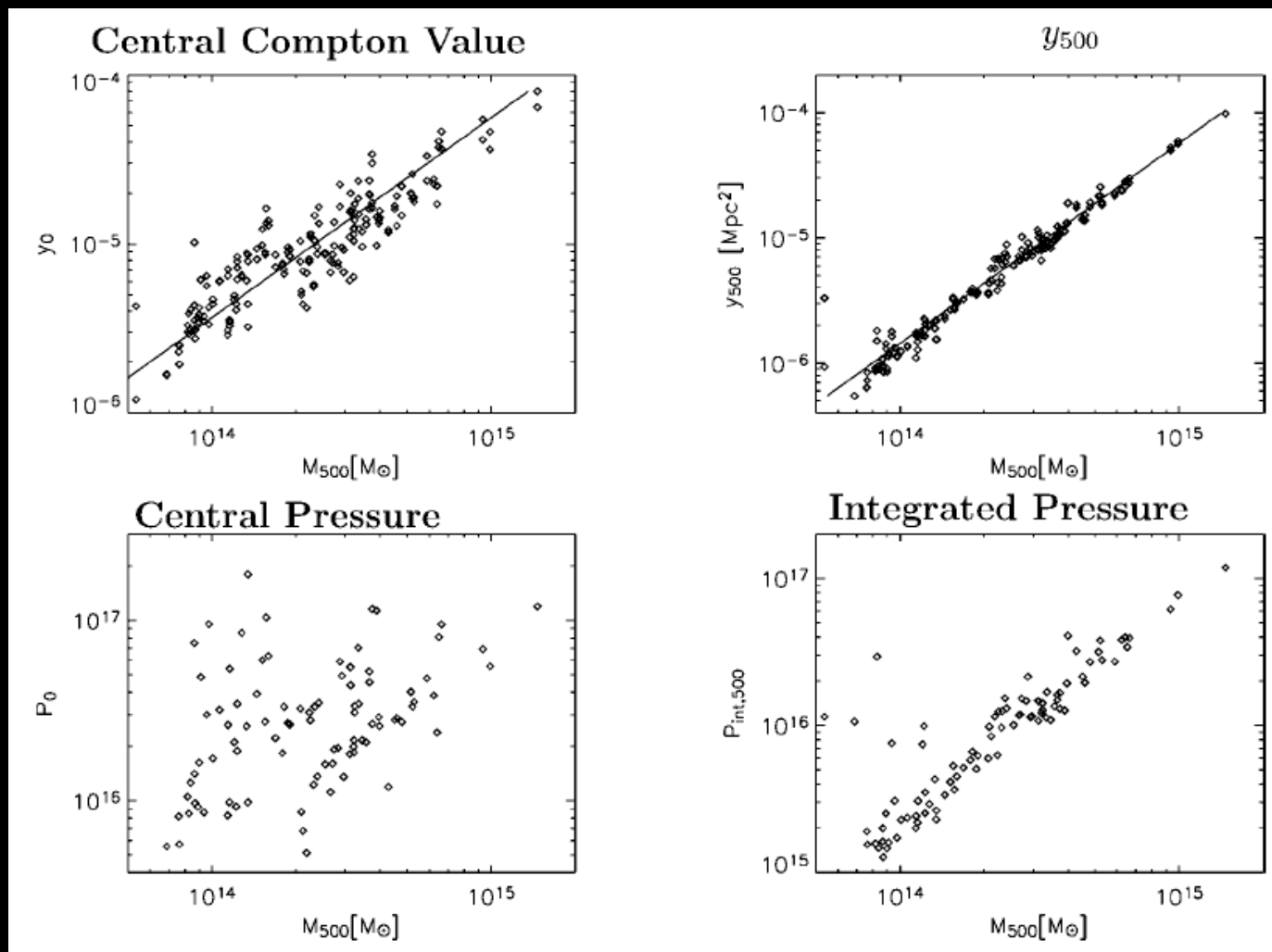
## Aside: calculating cluster masses from observables

- Accurate determination of cosmological parameters requires precise knowledge of cluster mass function  $n(>M, z)$
- This requires a well-understood relationship between  $M_{\text{gas}}/M_{\text{tot}}$  and at least one SZE observable ( $y_0, y_{500}$ , etc.)
- This observable-mass relationship must be reliable at 1) moderate resolution and 2) for a huge number of clusters ( $10^3$ - $10^4$  or more)

## Aside: calculating cluster masses from observables

- Historically, galaxy cluster masses deduced by using X-ray temperature or X-ray luminosity
- This is problematic for SZE surveys: X-ray telescope time is scarce, and lots of scatter for low-mass clusters
- SZE: possible observables are  $y_0$ ,  $y_{500}$  (or some other integrated  $y$  value). What sort of scatter do we observe?

# Motl et al. 2005, ApJ, 623, L63-66



$$10^{14} \lesssim M_{cl} \lesssim 2 \times 10^{15} M_{\odot}$$

# Motl et al. 2005, ApJ, 623, L63-66

TABLE 1

SCALING EXPONENT FOR  $y_{500}$ - $M$  RELATION,  $z = 0$

Simulation	$\alpha$	$\sigma_\alpha$
Adiabatic .....	1.59	0.021
Radiative cooling .....	1.71	0.031
Star formation .....	1.60	0.027
Star formation with feedback .....	1.61	0.024

Scaling depends on physics included in sims  
(baryonic physics important)

$y_{500}$ - $M$  seems most  
accurate scaling  
relation

TABLE 2

ACCURACY OF MASS ESTIMATION,  $z = 0$

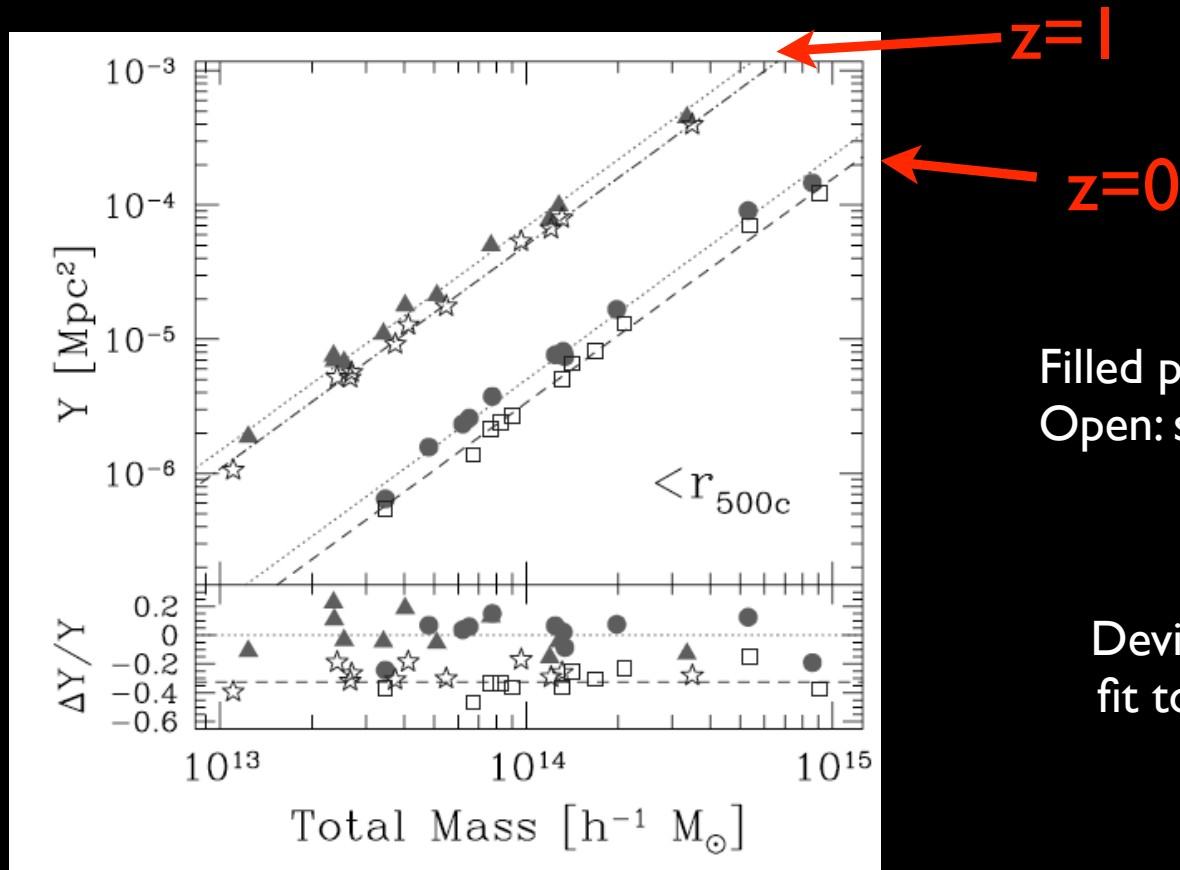
Method	Median $M_{\text{est}}/M_{\text{true}}$	+1 $\sigma$	-1 $\sigma$	+80%	-80%
$y_{500}$ - $M$ .....	0.97	1.00	0.93	1.13	0.86
$T_X$ - $M$ .....	1.04	1.11	0.92	1.33	0.74
$L_{X,500}$ - $M$ .....	0.87	1.03	0.75	1.46	0.62
$y_0$ - $M$ .....	0.96	1.14	0.82	1.53	0.67

$$10^{14} \lesssim M_{\text{cl}} \lesssim 2 \times 10^{15} M_{\odot}$$

# Nagai 2006, ApJ, 650, 538-49

## Self-similar SZE scaling relation

$$Y^{\text{int}} \propto \begin{cases} f_{\text{gas}} M^{5/3} E^{2/3}(z) \\ f_{\text{gas}} T^{5/2} E^{-1}(z) \end{cases}$$



Filled points: adiabatic  
Open: star formation+FB

Deviation from best  
fit to adiabatic runs



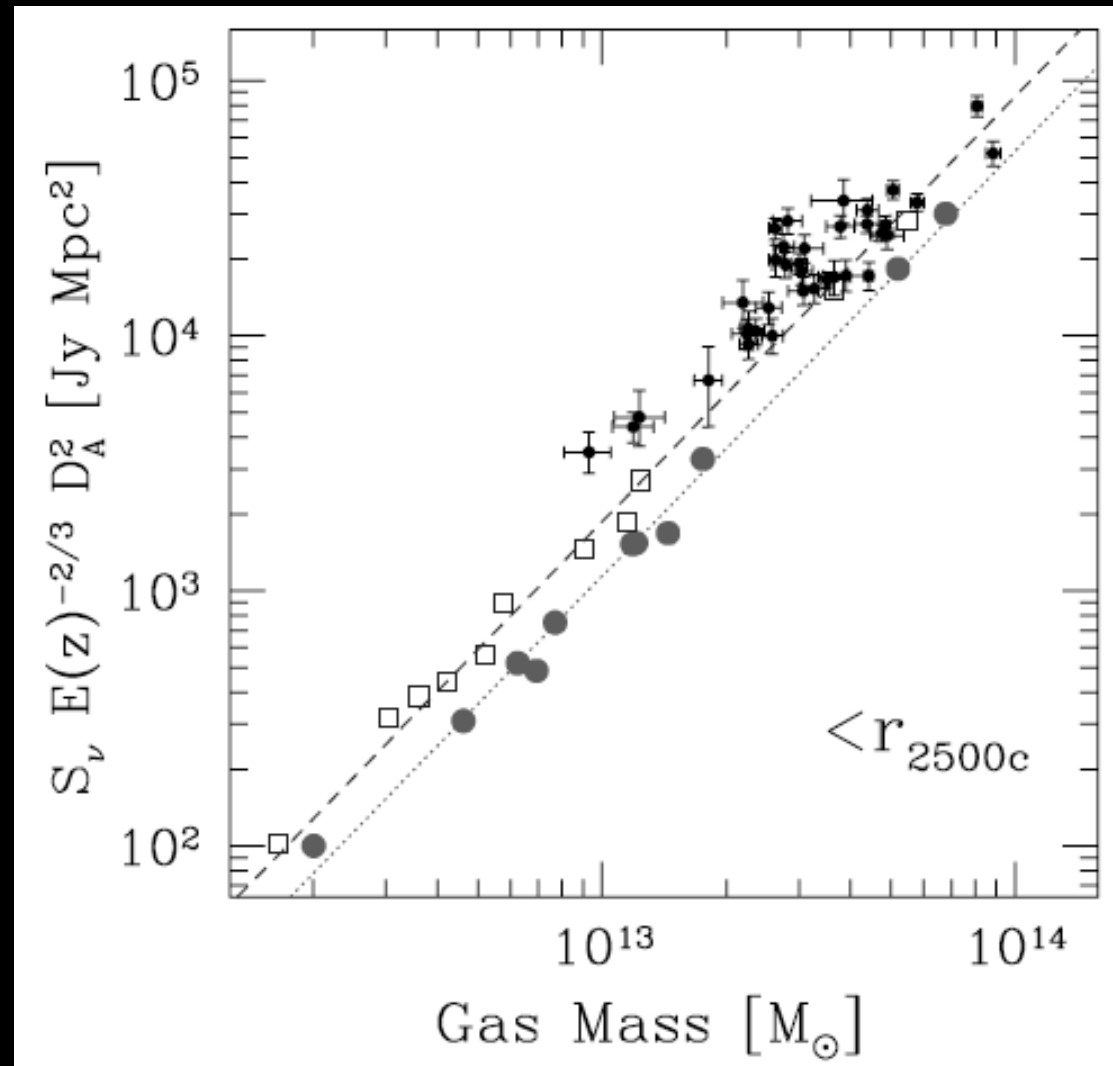
# Nagai 2006, ApJ, 650, 538-49

Points w/error bars:  
LaRoque 2005 (35  
clusters,  $0.14 < z < 0.89$ )

open squares: cooling  
+SF/FB sims

filled circles: adiabatic  
sims

Note: using gas mass  
within  $r_{2500}$



# Hubble constant, cosmological distance determination

- Distance to a galaxy cluster can be determined using a combination of SZE and X-ray emission (Cavaliere et al. 1977, Gunn et al. 1978, Birkinshaw 1979, etc.)
- Use different density dependencies of SZE, X-ray emission!

$$\Delta T_{SZE} \sim \int d\ell n_e T_e \qquad S_x \sim \int d\ell n_e^2 \Lambda_{eH}$$

# Hubble constant, cosmological distance determination

say  $d\ell = D_A d\zeta$

See Birkinshaw & Hughes (1994), Reese et al. (2000) for detailed derivations

so,  $\Delta T_{CMB,0} \sim n_{e,0} T_{e,0} D_A \int d\zeta$

and  $S_{X,0} \sim n_{e,0}^2 \Lambda_{eH0} D_A \int d\zeta$

and thus,  $D_A \sim \frac{\Delta T_{CMB,0}^2 \Lambda_{eH0}}{S_{X0} T_{e0}^2} \frac{1}{\Theta_c}$   $\Theta_c = \text{cluster scale along LOS}$

“0” subscripts: through center of cluster

$D_A + z_{cl} + k = \text{Hubble parameter!}$

# Two assumptions made in distance determinations!

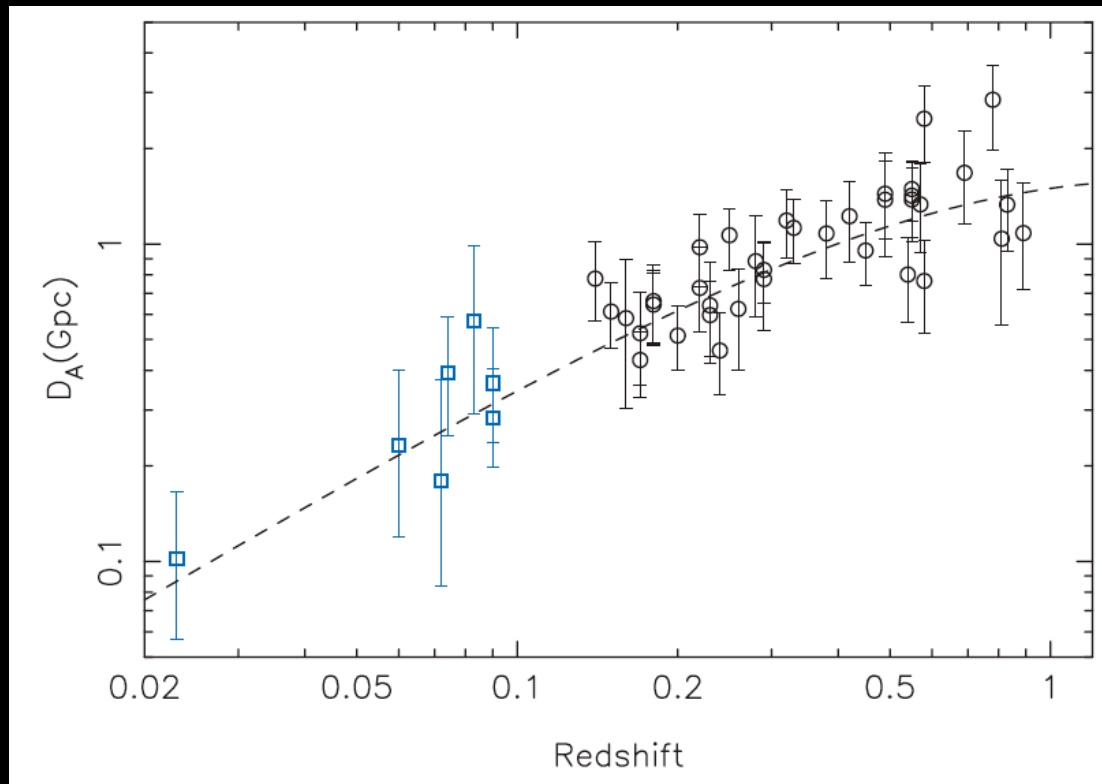
- Characteristic scale of cluster along LOS related to scale in plane of sky (symmetry)

Probably true in absence of selection effects

- $\langle n_e \rangle^2 = \langle n_e^2 \rangle$  along LOS ( $C = 1$ )

If this is not true,  $H \sim C^2$

# Results



Fit for 38 clusters (circles)  
dashed line: best-fit assuming  $\Omega_m = 0.3$   
 $\Omega_\Lambda = 0.7$

Bonamente et al. 2006,  
ApJ, 647, 25-54

38 clusters measured in  
SZE (OVRO/BIMA) and  
X-ray (Chandra) over  
 $0.14 \lesssim z \lesssim 0.89$

$H_0 = 76.9 \text{ km/s/Mpc}$  (+-  
 $\sim 12 \text{ km/s}$ ) assuming  
 $\Omega_m = 0.3$   $\Omega_\Lambda = 0.7$

(WMAP III best-fit:  $H_0 =$   
70.4,  $\Omega_m = 0.268$   
 $\Omega_\Lambda = 0.732$ )

# H, $D_A$ measurements: the future

- Statistical errors to be reduced: lots of clusters will be observed in both SZE, X-ray in near future
- Systematic errors all being examined:
  - departure from isothermality
  - clumping (substructure)
  - point source contamination of SZE
  - See Birkinshaw (1999), Reese et al. (2000, 2002)

# Cluster gas mass fraction

- The ICM contains most of the baryons within a cluster:  $f_g$  a reasonable approx. of baryonic mass fraction of cluster
- $f_g$  should also be approximately the universal mass fraction,  $f_B \equiv \Omega_B/\Omega_M$  (really,  $f_g \leq f_B$ )
- $f_B \rightarrow \Omega_M$ , given prior knowledge of  $\Omega_B$  (from BBN)

# How do we get $f_g$ ?

- Get  $M_g$  directly from SZE, assuming  $T_e$  is known (recall integrated SZE  $\sim M_g \langle T_e \rangle / D_A^2$ )
- Get  $M_{\text{tot}}$  by assuming hydrostatic equilibrium + observed gas distribution +  $T_e$  (or strong/weak lensing)
- Combined, this tells us  $f_g \sim \frac{\Delta T_{\text{SZE}}}{T_e^2}$



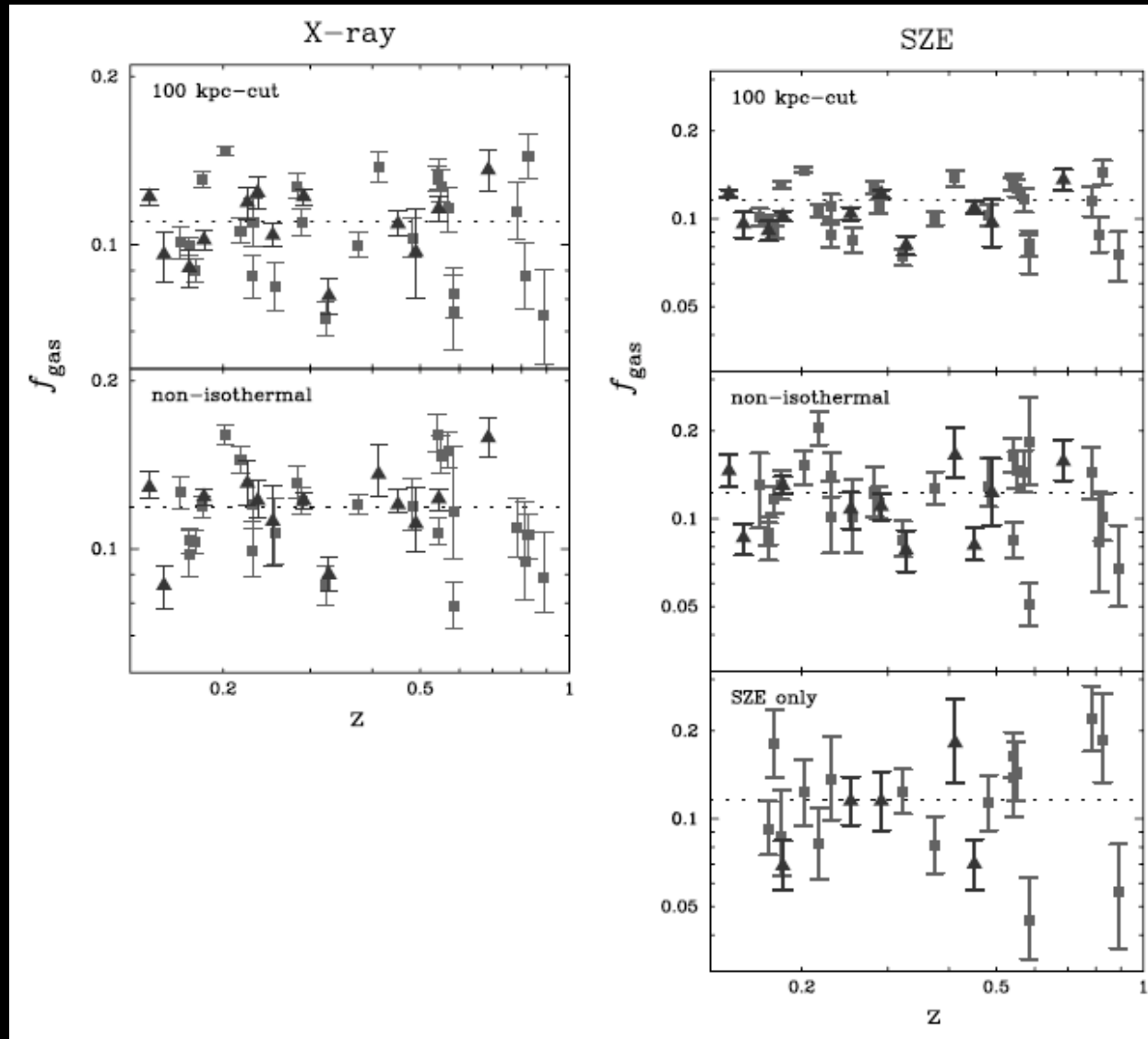
# Recent results: LaRoque et al. 2006, ApJ, 652, 917

Chandra + OVRO/  
BIMA data

38 galaxy clusters at  
 $0.14 < z < 0.89$

multiple fits to data

results agree with  
standard LCDM



# Problems with this method

- Observations strongly depend on X-ray, SZE systematics
- The assumption of hydrostatic equilibrium is a very dangerous one (and generally wrong - see later discussion)
- Standard isothermal, beta-model fits of density, temperature profiles are not accurate (Hallman et al. 2007; astro-ph/0705.0531)
- $f_g$  probably does not represent the cosmic mean at the 10% level (messy astrophysics)

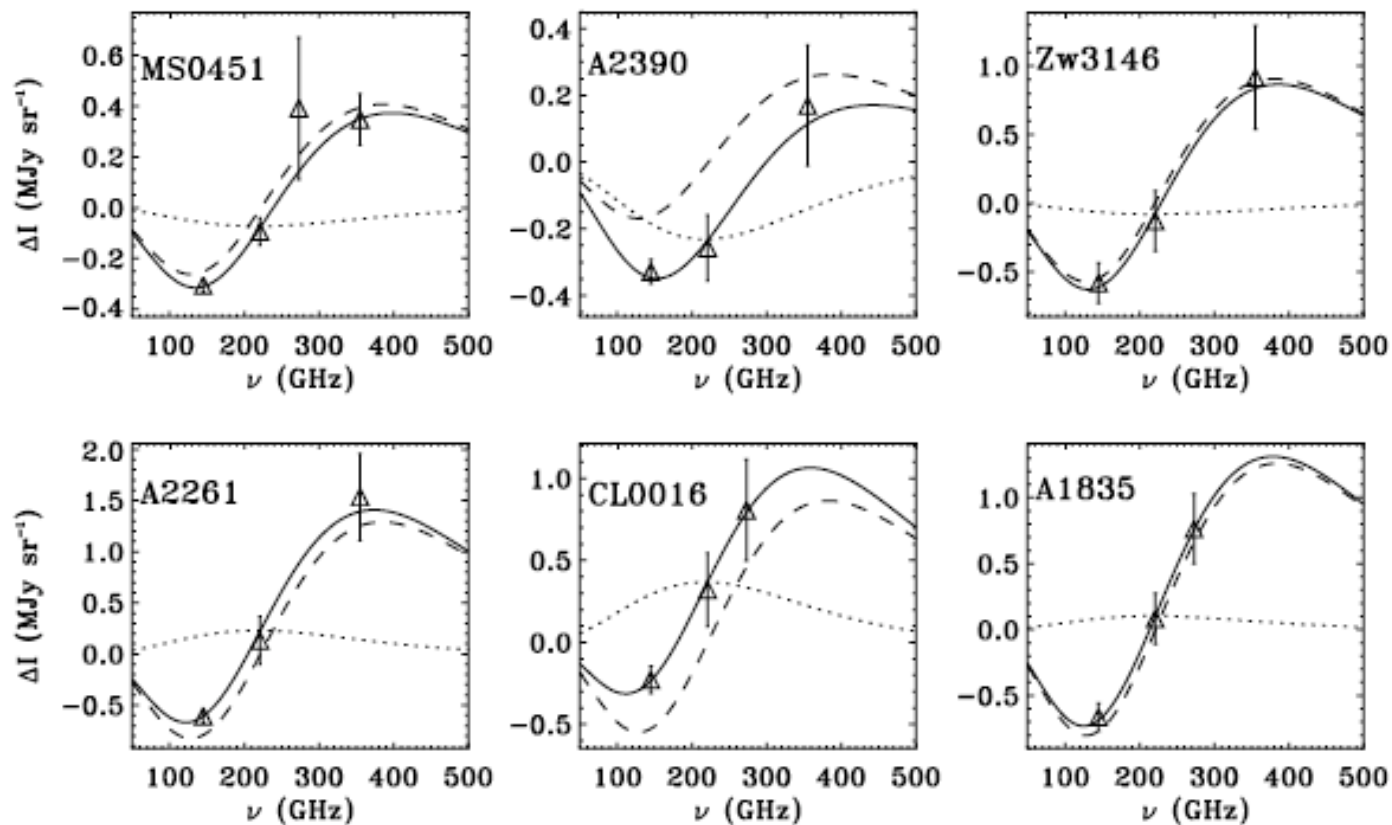
# Cluster peculiar velocities

- kinetic SZE: only known way to measure large-scale velocity fields at high  $z$
- cluster PV stats can constrain fundamental cosmological parameters - see talk later today by S. Bhattacharya
- sensitive multifrequency SZE obs'ns required to separate thermal, kinetic SZE (but possible w/ Planck)
- challenging due to contamination from CMB temperature fluctuations, other sources - however, averaging over many clusters may help

Recent(ish) results: Benson et al. 2003, ApJ, 592,  
674-691

- Made measurements of six galaxy clusters at  $z > 0.2$  using the SuZIE II SZE experiment
- Observe simultaneously at 3 frequency bands (centered on 145, 221, 355 GHz)
- Use measurements at these three bands, back out separate thermal, kinetic SZE components

# Recent(ish) results: Benson et al. 2003, ApJ, 592, 674-691



# Recent(ish) results: Benson et al. 2003, ApJ, 592, 674-691

TABLE 6  
SUMMARY OF RESULTS

Cluster	Date	$\Delta R.A.$ (arcsec)	$y_0 \times 10^4$	$v_{\text{pec}}$ (km s <sup>-1</sup> )
A2261 .....	1999 Mar	$6.4^{+18.6}_{-19.5}$	$7.41^{+1.95}_{-1.98}$	$-1575^{+1500}_{-975}$
A2390 .....	2000 Nov	$-4.8^{+18.1}_{-19.1}$	$1.72^{+1.01}_{-0.76}$	$+1900^{+6225}_{-2650}$
Zw 3146 .....	2000 Nov	$11.4^{+30.9}_{-30.9}$	$3.62^{+1.83}_{-2.52}$	$-400^{+3700}_{-1925}$
A1835 .....	1996 Apr	$28.0^{+16.0}_{-15.0}$	$7.66^{+1.64}_{-1.66}$	$-175^{+1675}_{-1275}$
Cl0016.....	1996 Nov	$6.2^{+34.5}_{-37.4}$	$3.27^{+1.45}_{-2.86}$	$-4100^{+2650}_{-1625}$
MS 0451.....	1996 Nov	$-15.5^{+26.0}_{-24.0}$	$3.20^{+1.61}_{-1.61}$	$+175^{+5750}_{-2625}$
	1997 Nov	$12.0^{+10.0}_{-11.0}$	$2.07^{+0.70}_{-0.72}$	$+1775^{+3900}_{-2150}$
	2000 Nov	$-21.5^{+21.0}_{-19.0}$	$3.17^{+0.86}_{-0.88}$	$-300^{+1950}_{-1275}$
Combined fit for MS 0451 .....			$2.84^{+0.52}_{-0.52}$	$+800^{+1525}_{-1125}$

## Recent(ish) results: Benson et al. 2003, ApJ, 592, 674-691

- Peculiar velocity values are really upper limits (given fitting method)
- Can use cluster sample to set limit on bulk flow in direction of CMB dipole:  $< 1420$  km/s at 95% CL
- Systematic uncertainties in peculiar velocity determination most likely dominated by submm point sources

# Outline

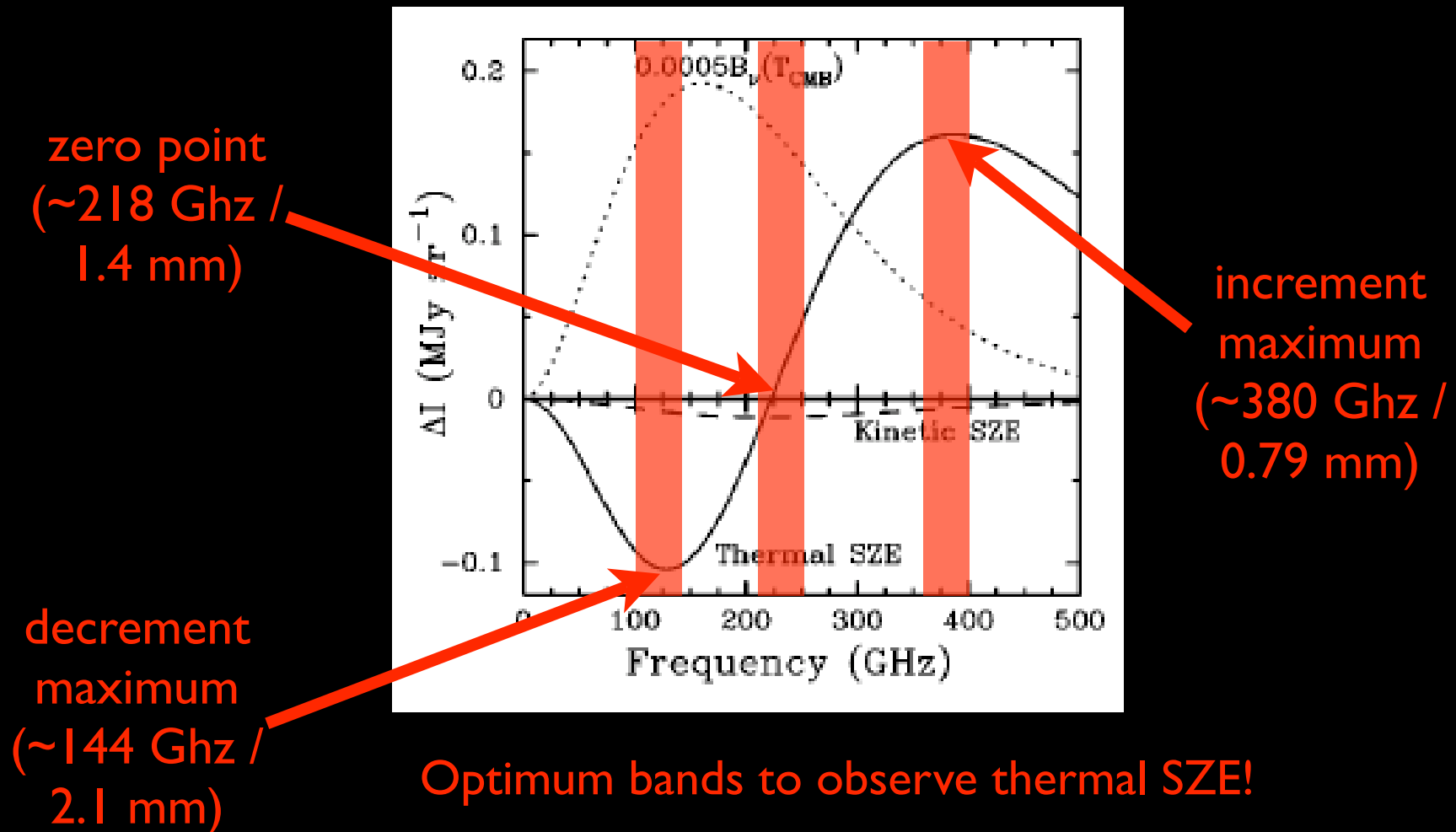
- (1) Some background: the CMB, inverse Compton scattering, galaxy clusters
- (2) The Sunyaev-Zel'dovich Effect
- (3) Cosmological probes
- (4) Upcoming SZ observational campaigns
- (5) Simulations of the SZE



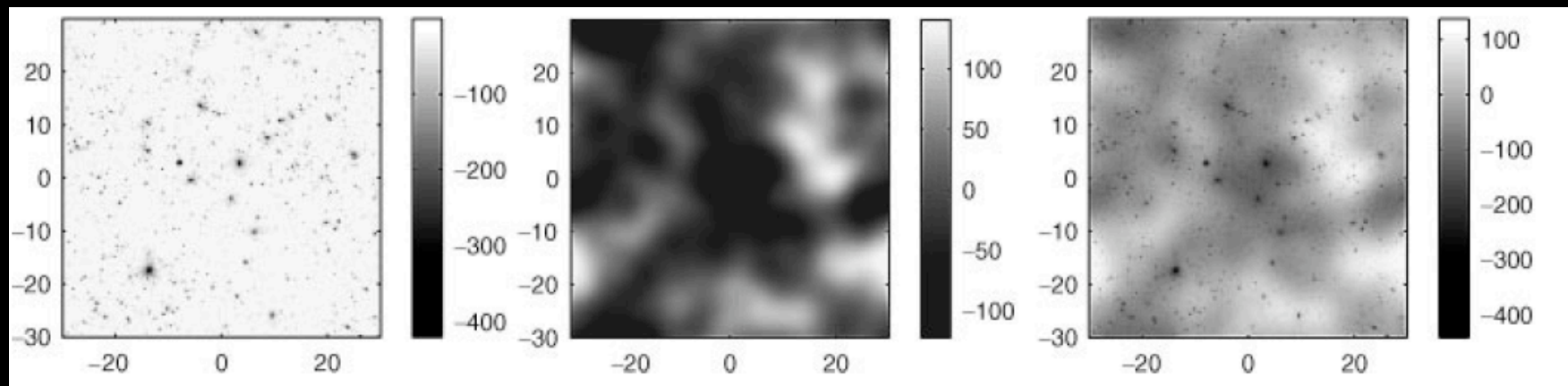
# Upcoming SZE obs. campaigns

- As discussed previously, the SZE can be a powerful cosmological probe
- Several SZE-specific mm-wave survey telescopes are currently under construction/seeing first light
- Will discuss ONLY single-dish telescopes in this section (see S. Myers talk from Monday re: uses of interferometers)

# First, a comment on SZE observations...



# Disentangling the SZE from primary CMB fluctuations



SZE @ 150 GHz

Primary CMB  
anisotropies  
@ 150 GHz

SZE + CMB  
@ 150 GHz

Image from Carlstrom et al. 2002, ARAA

Image 1 deg<sup>2</sup>

# Atacama Pathfinder Experiment SZ telescope (APEX-SZ)

- Collaboration between MPIfR, Onsalo Space Observatory, ESO
- Located in the Atacama desert in Chile: elev. 5100 m
- modified ALMA prototype antenna; 12 m dish
- Obs. at 1.4, 2 mm (218, 144 GHz) with beam FWHM of 1.0' and sensitivity of 10  $\mu$ K @ 144 GHz
- Survey  $\sim 200$  deg<sup>2</sup> over two seasons - online now!
- <http://www.apex-telescope.org/>

# South Pole Telescope (SPT)

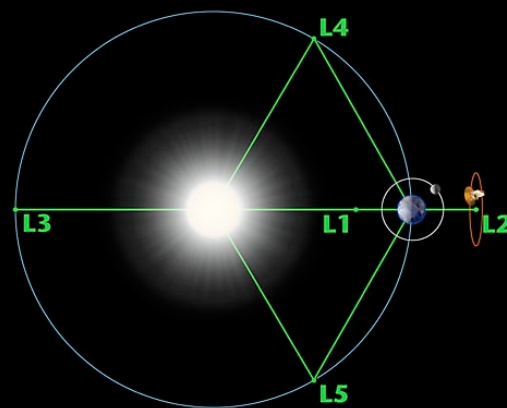
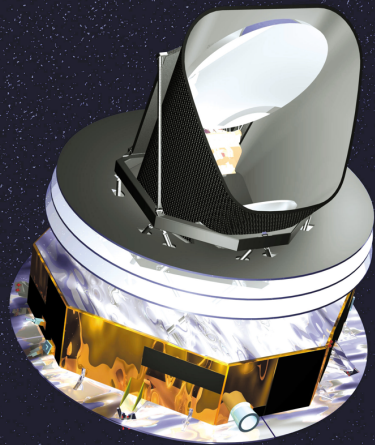
- Collaboration of various US universities, lead by U of Chicago
- Located at South Pole, completed Jan. 2007 (First light Feb. 16, 2007)
- 10m primary mirror, very sensitive bolometer array
- Survey  $\sim 4000 \text{ deg}^2$  over 1-3mm ( $\sim 100\text{-}300 \text{ GHz}$ ) range (90, 150, 220, 270 GHz channels)
- Beam FWHM of 1.0' and sensitivity of 10  $\mu\text{K}$  @ 150 GHz
- <http://spt.uchicago.edu/>

# Atacama Cosmology Telescope (ACT)

- International collaboration: US, Canada, Mexico, Chile, South Africa, UK
- Telescope located in Atacama Desert, Chile (elev. 5100 m),
- Observe 2 deg. strip x 50 deg. long (100 deg<sup>2</sup>) at 150, 220, 270 GHz over 2 years (First light late 2007)
- Beam FWHM of 1.0' and sensitivity of 2  $\mu$ K @ 150 GHz
- <http://www.physics.princeton.edu/act/>

# Planck Surveyor

- Satellite mission funded by ESA
- Launching July/August 2008, final location L2
- nominal mission length 12-14 months (on-station), results in 2010
- see <http://www.rssd.esa.int/index.php?project=Planck> for more details



# Planck Surveyor

- 1.5m telescope (satellite), observing whole sky in 30-875 GHz frequency range (30, 44, 70, 100, 143, 217, 353, 545, 875 GHz) - including polarization!
- Resolution 7.1' @ 143 GHz, sens. 6  $\mu$ K RMS/beam
- Measure  $y$  in  $> 10^4$  clusters
- Measure bulk velocities of LSS (scales  $> 300$  Mpc) out to  $z \sim 1$  with  $dv \sim 50$  km/s
- Estimate  $H_0$  from SZE, X-ray



## Side-by-side comparison of single-dish SZE experiments

	Sky coverage (deg <sup>2</sup> )	Beam FWHM @ 144 GHz (arcmin)	RMS/Beam ( $\mu$ K)
APEX-SZ	200	1.0	10
SPT	4000	1.0	10
ACT	100	1.7	2
Planck	All-sky	7.1	6

# Outline

- (1) Some background: the CMB, inverse Compton scattering, galaxy clusters
- (2) The Sunyaev-Zel'dovich Effect
- (3) Cosmological probes
- (4) Upcoming SZ observational campaigns
- (5) Simulations of the SZE

# Why do we need simulations?

- “Precision cosmology” requires estimates of cluster mass (as it relates to observables) to high (percent-level) accuracy
- Analytic models typically assume clusters are very simple: hydrostatic, spherical, simple temperature profiles (isothermal or beta-model) and have limited physics
- We need to understand scatter+bias in SZE, X-ray, optical observables due to non-ideal (“realistic”) GCs in order to calibrate observations
- In general, fewer assumptions in simulations than in analytic models - more useful for comparing to observations!

# What can we *do* with simulations?

- Test scaling relations between observables and intrinsic cluster properties (e.g.  $L$ ,  $T$ ,  $y_0$ ,  $y_{500}$ ,  $Y$  vs.  $M_{\text{gas}}$ ,  $M_{\text{tot}}$ ,  $C$ , ...) and also potential *bias and scatter* in each observable
- Test the impact of dynamical events and non-ideal properties of clusters (mergers, asphericity) as well as the impact of new physics (gas, cooling, SF+FB, CRs, AGN, B-fields, conduction, etc...) on cluster properties (e.g. Pfrommer talk on Tuesday)
- Make mock observations to test analysis pipelines, etc. - can we get out the cosmology we put in?

# Some examples of galaxy cluster simulations...

(an embarrassingly incomplete list)

# Cluster SZE scaling relations

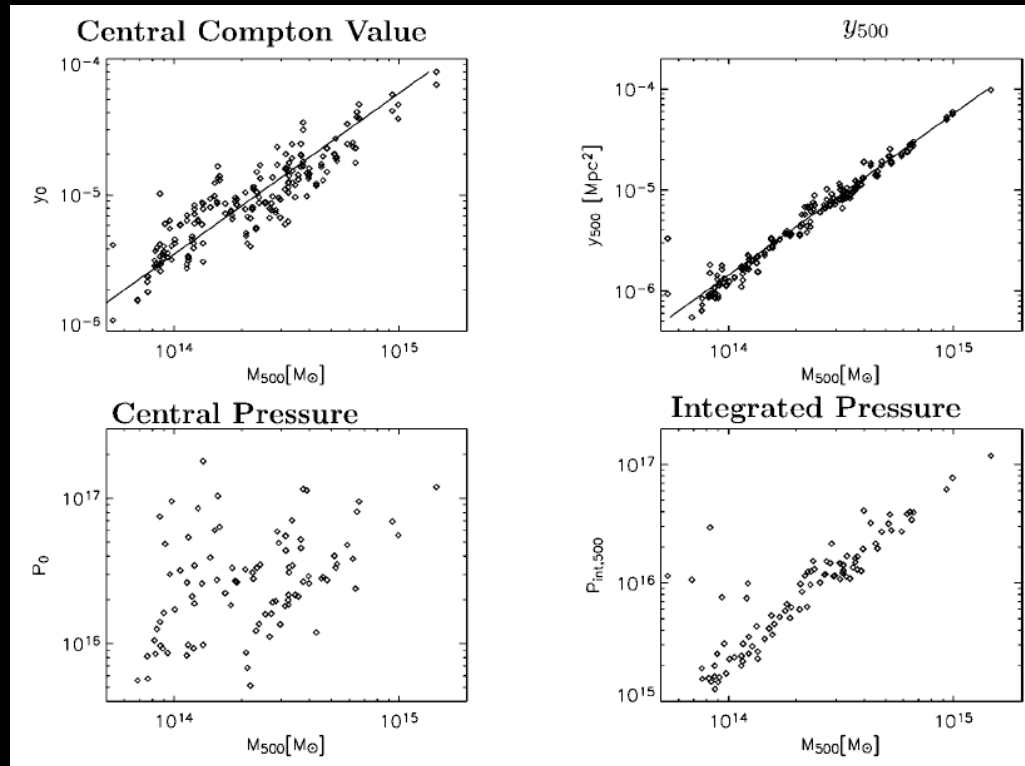


TABLE 1  
SCALING EXPONENT FOR  $y_{500}$ - $M$  RELATION,  $z = 0$

Simulation	$\alpha$	$\sigma_{\alpha}$
Adiabatic .....	1.59	0.021
Radiative cooling .....	1.71	0.031
Star formation .....	1.60	0.027
Star formation with feedback .....	1.61	0.024

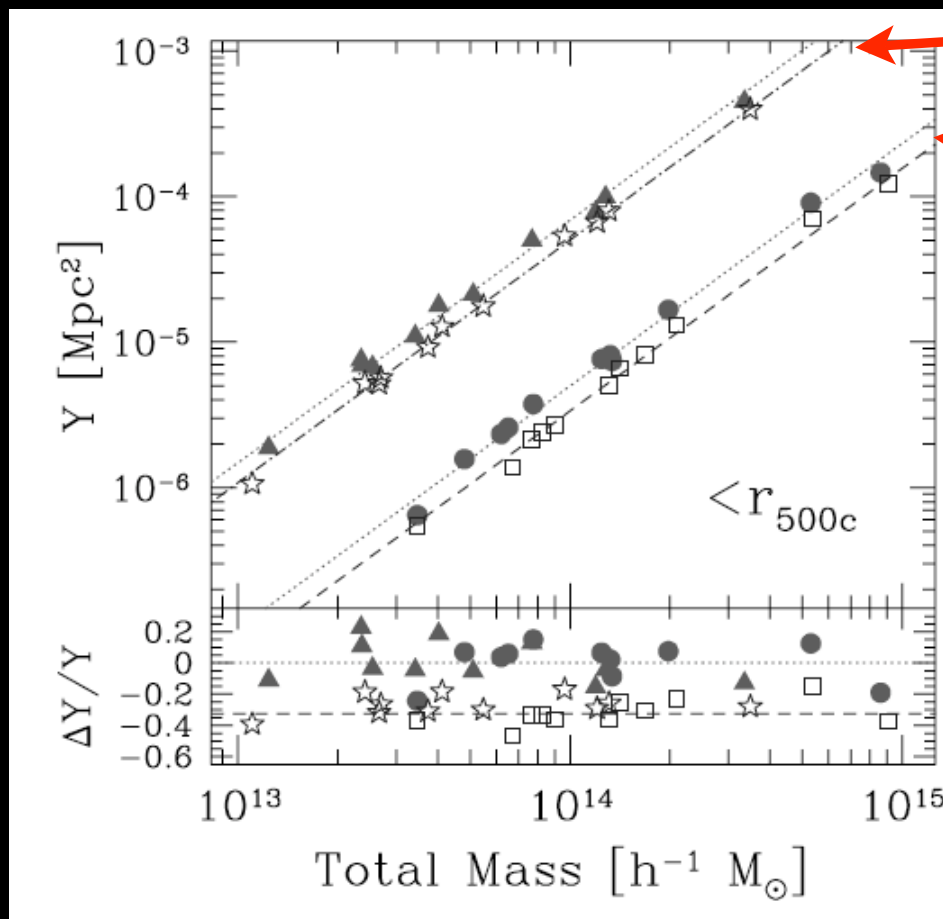
TABLE 2  
ACCURACY OF MASS ESTIMATION,  $z = 0$

Method	Median $M_{est}/M_{true}$	+1 $\sigma$	-1 $\sigma$	+80%	-80%
$y_{500}$ - $M$ .....	0.97	1.00	0.93	1.13	0.86
$T_x$ - $M$ .....	1.04	1.11	0.92	1.33	0.74
$L_{x,500}$ - $M$ .....	0.87	1.03	0.75	1.46	0.62
$y_0$ - $M$ .....	0.96	1.14	0.82	1.53	0.67

$$10^{14} \lesssim M_{cl} \lesssim 2 \times 10^{15} M_{\odot}$$

Motl et al. 2005, ApJ, 623, L63-66

# Cluster SZE scaling relations



$$Y^{\text{int}} \propto \begin{cases} f_{\text{gas}} M^{5/3} E^{2/3}(z) \\ f_{\text{gas}} T^{5/2} E^{-1}(z) \end{cases}$$

Filled points: adiabatic  
Open: star formation+FB

Deviation from best  
fit to adiabatic runs

Nagai 2006, ApJ, 650, 538-49

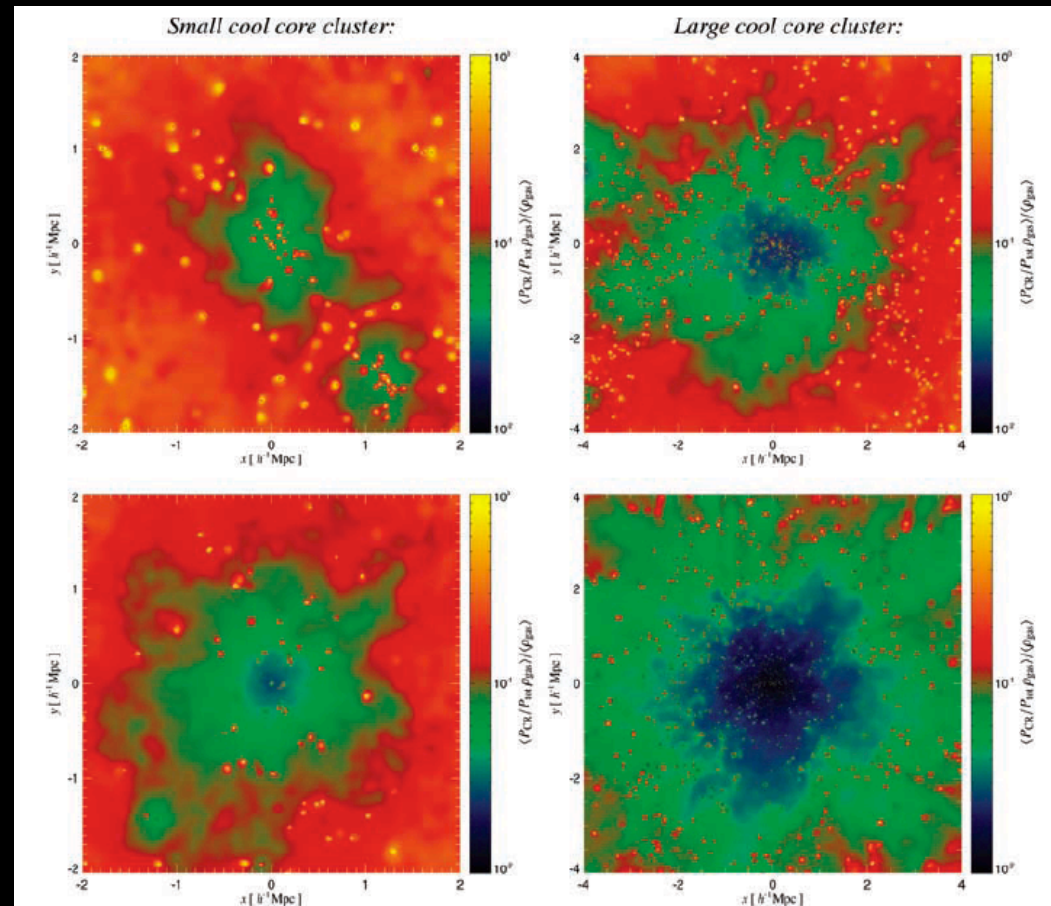
# Impact of new physics

## Cosmic rays

$z=1$

Shown: mass-weighted CR pressure relative to total pressure for two cool-core clusters, including CRs from structure formation shocks

$z=0$



$8.8 \times 10^{13} h^{-1} M_{\odot}$

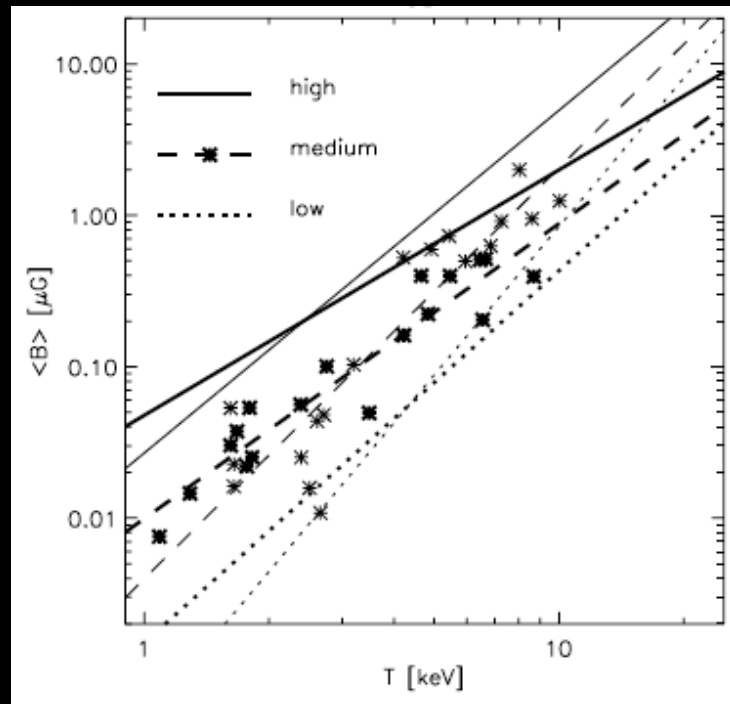
$1.8 \times 10^{15} h^{-1} M_{\odot}$

Pfrommer et al. 2007, MNRAS, 378, 385-408

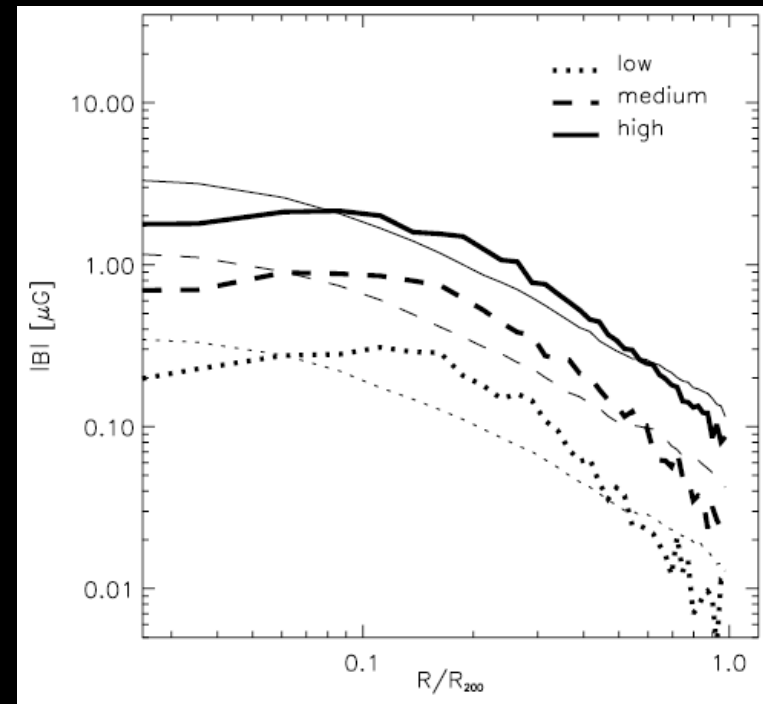


# Impact of new physics

## Magnetic fields

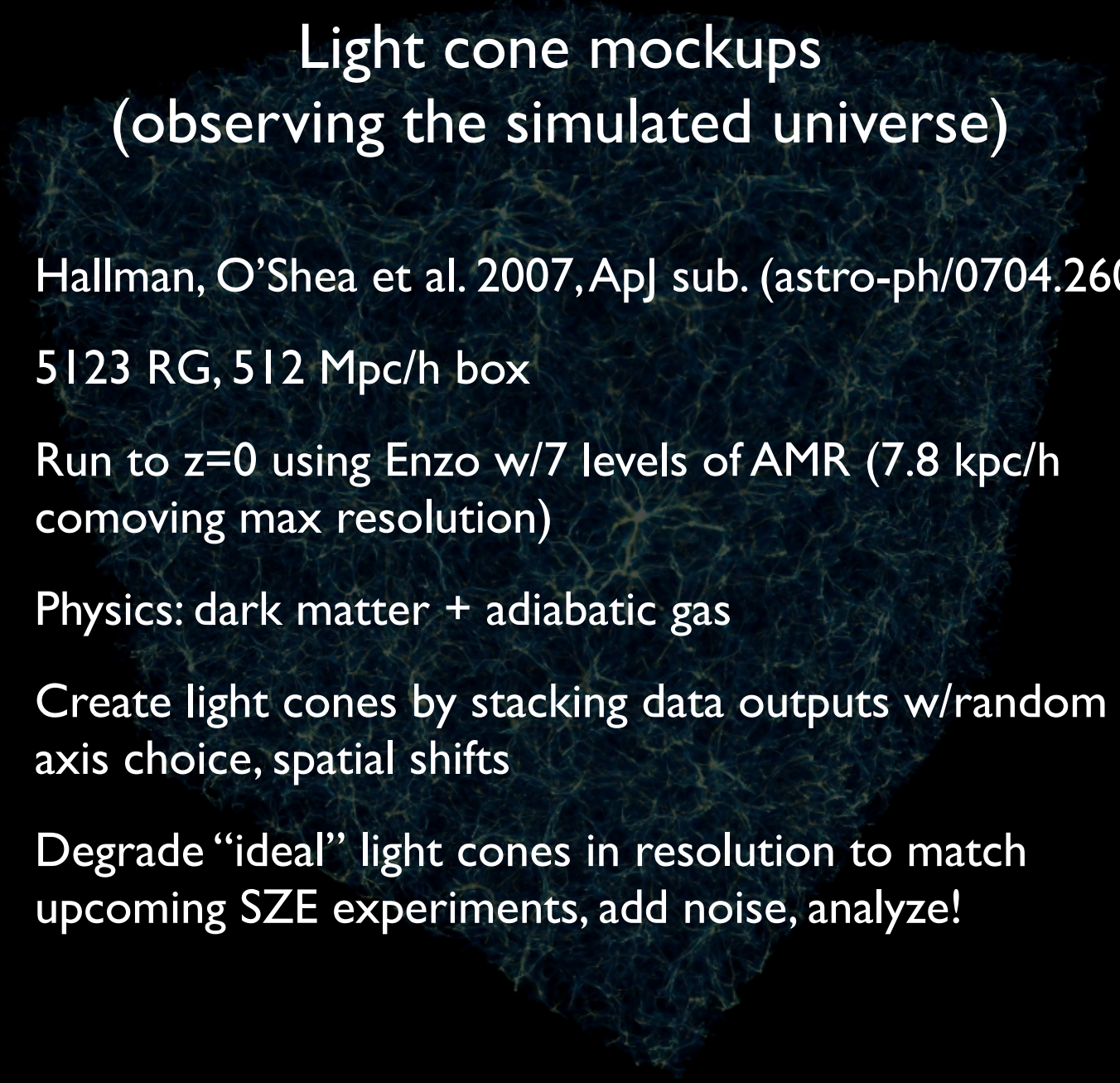


Mean B-field as fctn  
of cluster temp.



Mean B-field as fctn  
of radius

Dolag et al. 2002, A&A, 387, 383-95



## Light cone mockups (observing the simulated universe)

- Hallman, O'Shea et al. 2007, ApJ sub. (astro-ph/0704.2607)
- 5123 RG, 512 Mpc/h box
- Run to  $z=0$  using Enzo w/7 levels of AMR (7.8 kpc/h comoving max resolution)
- Physics: dark matter + adiabatic gas
- Create light cones by stacking data outputs w/random axis choice, spatial shifts
- Degrade “ideal” light cones in resolution to match upcoming SZE experiments, add noise, analyze!

# Light cone mockups (observing the simulated universe)

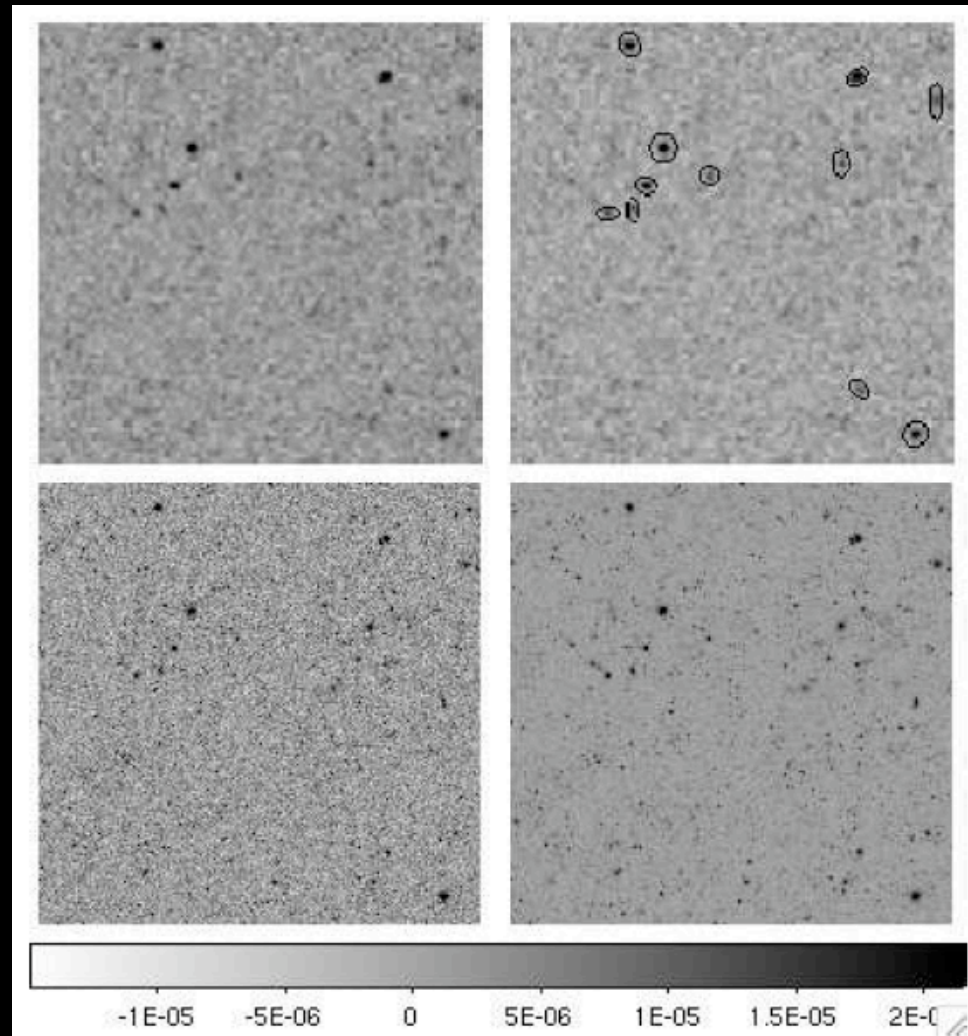
100 deg<sup>2</sup> field

Planck

APEX/SPT

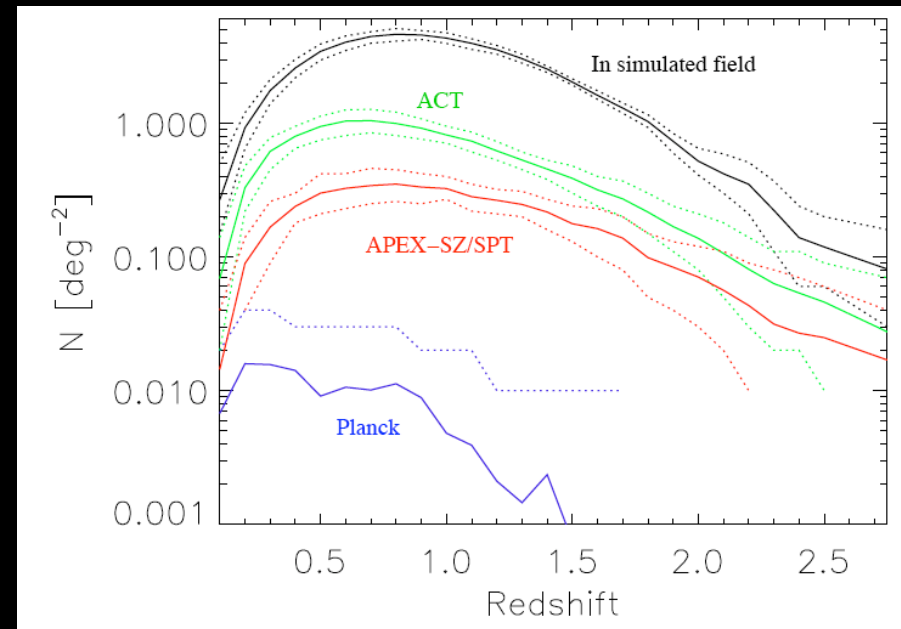
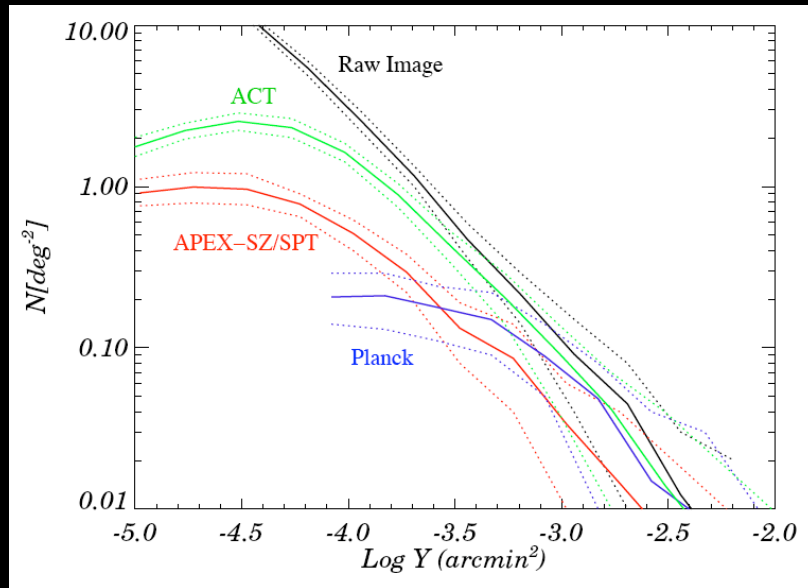
Planck w/  
sources

ACT

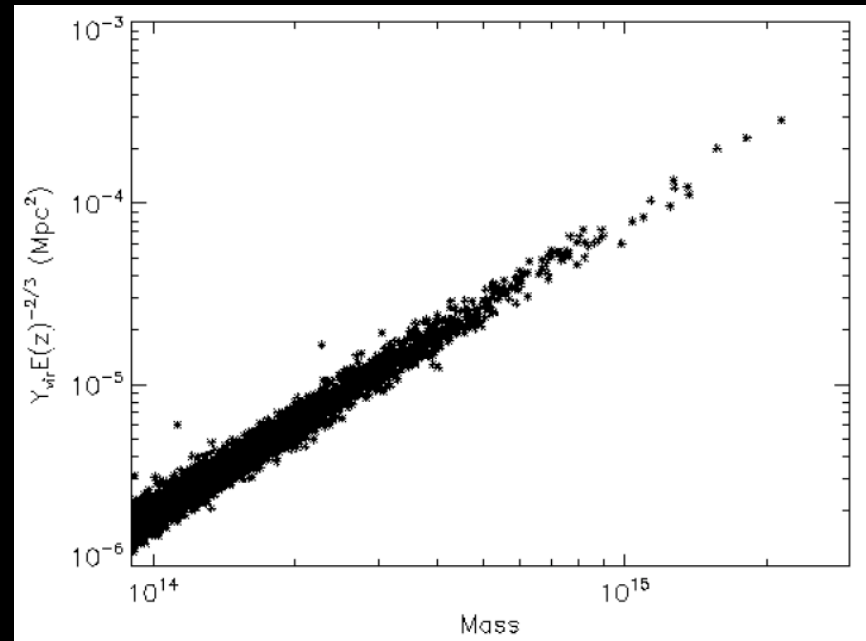
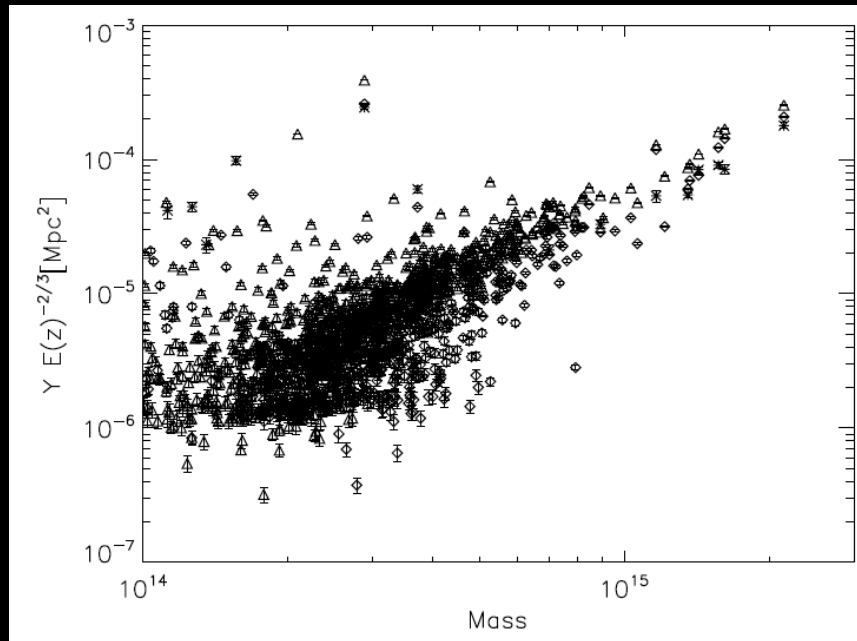


Hallman, O'Shea, et al. 2007, ApJ submitted (astro-ph/0704.2607)

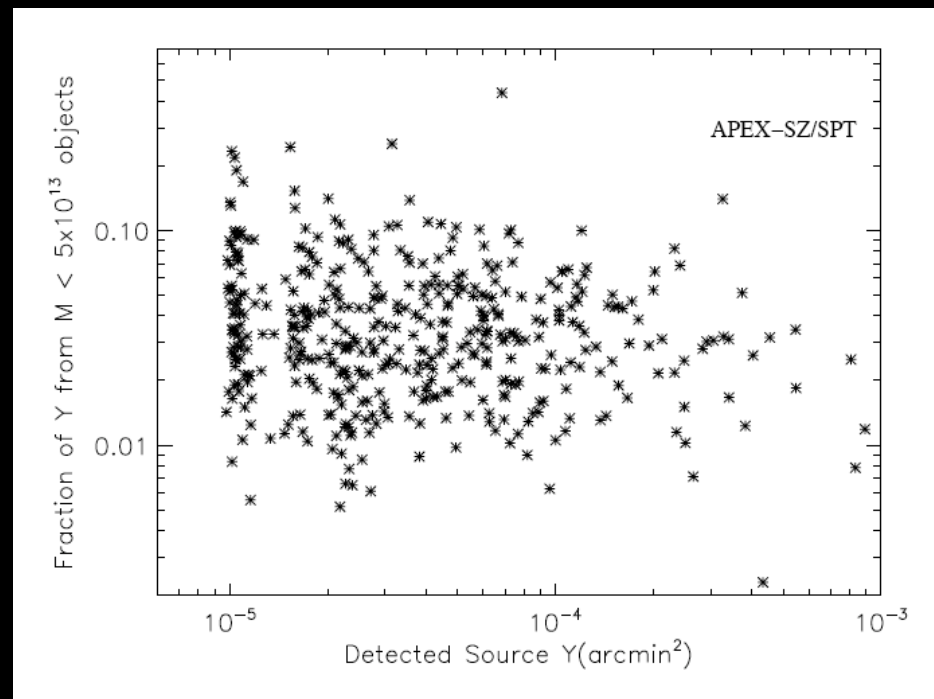
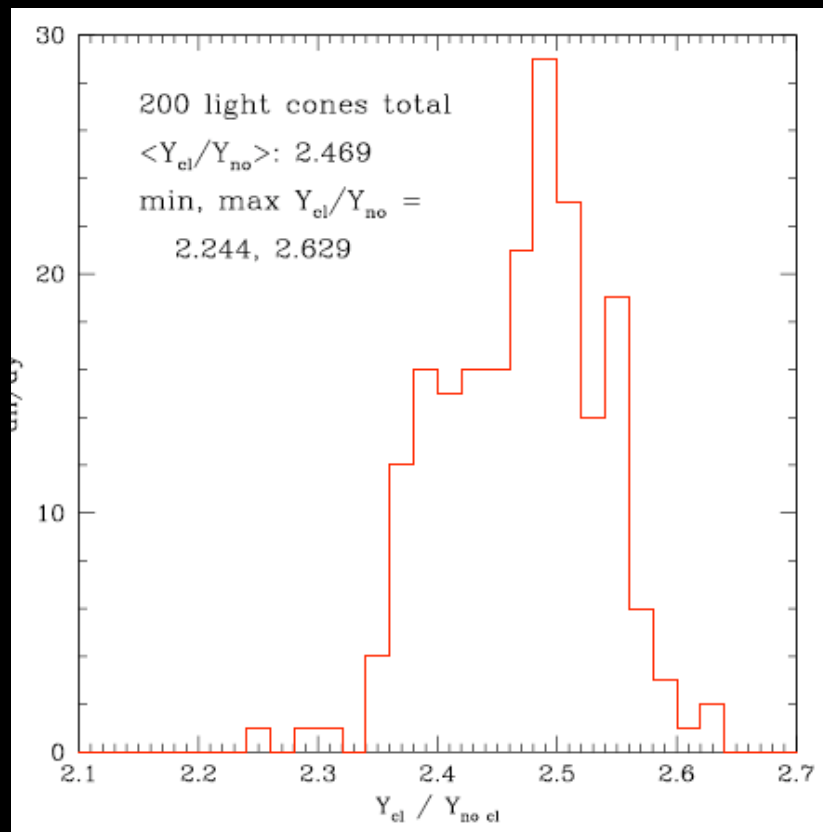
# Light cone mockups (observing the simulated universe)



# Light cone mockups (observing the simulated universe)



# Light cone mockups (observing the simulated universe)



# Conclusions

1. The Sunyaev-Zel'dovich effect has the potential to be an extremely powerful cosmological probe
2. Multiple facets: thermal SZE, kinetic SZE, polarization
3. The SZE can be used to probe galaxy cluster abundances and evolution ( $w, \Omega_m, \sigma_8$ ), cluster gas mass fractions ( $\Omega_m$ ), cluster distances ( $H_0$ ), cluster peculiar velocities (large-scale velocity statistics)

# Conclusions

4. Several complementary single-dish observational campaigns are currently underway or will be underway shortly, covering significant fractions of the sky: expect to find thousands of GCs!
5. These campaigns (and most of the cosmological probes discussed) require some sort of followup (optical with photo-z, X-ray) to be useful
6. Simulations show that many simplifying assumptions (spherical shapes, isothermality, hydrostatic equilibrium, etc.) are not true, so caution is needed to interpret SZE results



# Conclusions

7. Large-scale numerical simulations can be used to generate mock SZE observations, enabling the testing of data analysis pipelines and potentially uncovering observational challenges/opportunities

# Some useful references

- “*Cosmology with the Sunyaev-Zel'dovich Effect*,” Carlstrom, Holder & Reese, 2002 ARAA, 40:643-680
- “*CMB Anisotropies*,” Hu & Dodelson, 2002 ARAA 40:171-216
- “*Comptonization of the CMB: The Sunyaev-Zel'dovich Effect*,” Y. Rephaeli, 1995 ARAA 33:541-79